# DATA MINING 2 Performance Evaluation

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# https://www.wooclap.com/DM2EVAL

# **Metrics for Performance Evaluation**

- Focus on the predictive capability of a model
  - Rather than how fast it takes to classify or build models, scalability, etc.

• Confusion Matrix:

	PREDICTED CLASS					
		Class=Yes	Class=No			
ACTUAL	Class=Yes	а	b			
CLASS	Class=No	С	d			

a: TP (true positive)

- b: FN (false negative)
- c: FP (false positive)
- d: TN (true negative)

### Metrics for Performance Evaluation...

	PREDICTED CLASS					
		Class=Yes	Class=No			
ACTUAL	Class=Yes	a (TP)	b (FN)			
ULASS	Class=No	c (FP)	d (TN)			

Most widely-used metric:  

$$Accuracy = \frac{a+d}{a+b+c+d} = \frac{TP+TN}{TP+TN+FP+FN}$$

# Limitation of Accuracy

- Consider a 2-class problem
  - Number of Class 0 examples = 9990
  - Number of Class 1 examples = 10
- If model predicts everything to be class 0, accuracy is 9990/10000 = 99.9 %
  - Accuracy is misleading because model does not detect any class 1 example

### Cost Matrix

	PREDICTED CLASS				
	C(i j)	Class=Yes	Class=No		
ACTUAL	Class=Yes	C(Yes Yes)	C(No Yes)		
CLASS	Class=No	C(Yes No)	C(No No)		

C(i|j): Cost of misclassifying class j example as class i

# **Computing Cost of Classification**

Cost Matrix	PREDICTED CLASS				
	C(i j)	+	-		
ACTUAL	+	-1	100		
OLAGO		1	0		

Model M <sub>1</sub>	PREDICTED CLASS			
		+	-	
ACTUAL	+	150	40	
	-	60	250	

Model M <sub>2</sub>	PREDICTED CLASS			
		+	-	
ACTUAL	+	250	45	
02,000		5	200	

Accuracy = 80% Cost = 3910 Accuracy = 90% Cost = 4255

### Cost vs Accuracy

Count	PREDICTED CLASS				
		Class=Yes	Class=No		
ACTUAL CLASS	Class=Yes	а	b		
	Class=No	С	d		

Cost	PREDICTED CLASS				
		Class=Yes	Class=No		
ACTUAL CLASS	Class=Yes	р	q		
	Class=No	q	р		

Accuracy is proportional to cost if 1 - C(Vac|Na) = C(Na|Na) = C(Na) = C(

1. C(Yes|No)=C(No|Yes) = q 2. C(Yes|Yes)=C(No|No) = p

N = a + b + c + d

Accuracy = (a + d)/N

### **Cost-Sensitive Measures**

Precision (p) = 
$$\frac{TP}{TP + FP}$$
  
Recall (r) =  $\frac{TP}{TP + FN}$   
F-measure (F) =  $\frac{2rp}{r + p} = \frac{2TP}{2TP + FN + FP}$ 

- Precision is biased towards C(Yes|Yes) & C(Yes|No)
- Recall is biased towards C(Yes|Yes) & C(No|Yes)
- F-measure is biased towards all except C(No|No)

Weighted Accuracy = 
$$\frac{w_1 a + w_4 d}{w_1 a + w_2 b + w_3 c + w_4 d}$$

# Data Partitioning

Dataset			
Train	Train		
Train the model for final testing			
Train	Validation	Test	
Train the model for parameter selection	Validate the model (early stopping, parameter selection, etc.)	<ul> <li>Test the model</li> <li>Compare difference models once parameters hav been selected</li> </ul>	ent e
		Test	

Cross Validation (check potential dataset bias)



# **ROC (Receiver Operating Characteristic)**

- Developed in 1950s for signal detection theory to analyze noisy signals
  - Characterize the trade-off between positive hits and false alarms
- ROC curve plots TP (on the y-axis) against FP (on the x-axis)
- Performance of each classifier represented as a point on the ROC curve
  - changing the threshold of algorithm, sample distribution or cost matrix changes the location of the point

# Receiver Operating Characteristic Curve

- It illustrates the ability of a binary classifier as its discrimination threshold THR is varied.
- The *ROC* curve is created by plotting the true positive rate (TPR) against the false positive rate (FPR) at various THR.
- The TPR = TP / (TP + FN) is also known as sensitivity, recall or probability of detection.
- The FPR = FP / (TN + FP) is also known as probability of *false alarm* and can be calculated as (1 – specificity).



## **ROC Curve**

- 1-dimensional data set containing 2 classes (positive and negative)

- any points located at x > t is classified as positive



# **ROC Curve**

#### (TP,FP):

- (0,0): declare everything to be negative class
- (1,1): declare everything to be positive class
- (0,1): ideal
- Diagonal line:
  - Random guessing
  - Below diagonal line:
    - prediction is opposite of the true class



## Using ROC for Model Comparison



- No model consistently outperform the other
  - M<sub>1</sub> is better for small FPR
  - M<sub>2</sub> is better for large FPR
- Area Under the ROC curve
  - Ideal:
    - Area = 1
  - Random guess:
    - Area = 0.5

### How to Construct a ROC curve

Instance	P(+ A)	True Class
1	0.95	+
2	0.93	+
3	0.87	-
4	0.85	-
5	0.85	-
6	0.85	+
7	0.76	-
8	0.53	+
9	0.43	-
10	0.25	+

• Use classifier that produces posterior probability for each test instance P(+|A)

- Sort the instances according to P(+|A) in decreasing order
- Apply threshold at each unique value of P(+|A)
- Count the number of TP, FP, TN, FN at each threshold
- TP rate, TPR = TP/(TP+FN)
- FP rate, FPR = FP/(FP + TN)

### How to construct an ROC curve

	Class	+	-	+	-	-	-	+	-	+	+	
Threshold	>=	0.25	0.43	0.53	0.76	0.85	0.85	0.85	0.87	0.93	0.95	1.00
	ТР	5	4	4	3	3	3	3	2	2	1	0
	FP	5	5	4	4	3	2	1	1	0	0	0
	TN	0	0	1	1	2	3	4	4	5	5	5
	FN	0	1	1	2	2	2	2	3	3	4	5
	TPR	1	0.8	0.8	0.6	0.6	0.6	0.6	0.4	0.4	0.2	0
<b>→</b>	FPR	1	1	0.8	0.8	0.6	0.4	0.2	0.2	0	0	0



- The lift curve is a popular technique in direct marketing.
- The input is a dataset that has been "scored" by appending to each case the estimated probability that it will belong to a given class.
- The cumulative *lift chart* (also called *gains chart*) is constructed with the cumulative number of cases (descending order of probability) on the x-axis and the cumulative number of true positives on the y-axis.
- The dashed line is a reference line. For any given number of cases (the x-axis value), it represents the expected number of positives we would predict if we did not have a model but simply selected cases at random. It provides a benchmark against which we can see performance of the model.

Notice: "Lift chart" is a rather general term, often used to identify also other kinds of plots. Don't get confused!

## Lift Chart – Example

Serial no.	Predicted prob of 1	Actual Class	Cumulative Actual class
1	0.995976726	1	1
2	0.987533139	1	2
3	0.984456382	1	3
4	0.980439587	1	4
5	0.948110638	1	5
6	0.889297203	1	6
7	0.847631864	1	7
8	0.762806287	0	7
9	0.706991915	1	8
10	0.680754087	1	9
11	0.656343749	1	10
12	0.622419543	0	10
13	0.505506928	1	11
14	0.47134045	0	11
15	0.337117362	0	11
16	0.21796781	1	12
17	0.199240432	0	12
18	0.149482655	0	12
19	0.047962588	0	12
20	0.038341401	0	12
21	0.024850999	0	12
22	0.021806029	0	12
23	0.016129906	0	12
24	0.003559986	0	12



# Lift Chart – Application Example

- From Lift chart we can easily derive an "economical value" plot, e.g. in target marketing.
- Given our predictive model, how many customers should we target to maximize income?
- Profit = UnitB\*MaxR\*Lift(X) UnitCost\*N\*X/100
- UnitB = unit benefit, UnitCost = unit postal cost
- N = total customers
- MaxR = expected potential respondents in all population (N)
- Lift(X) = lift chart value for X, in [0,..,1]

### Lift Chart – Application Example



### References

• Chapter 3. Classification: Basic Concepts and Techniques.



# Exercises – ROC & Lift Chart

### **ROC Exercise**



### **ROC Exercise Solution**



### Lift Exercise



### Lift Exercise Solution

