# Information Retrieval - EXERCISES 16 January 2024 - time 60 minutes 

## Name and Surname:

## \#matricola:

Question \#1 [scores 4] Show how it is compressed by the algorithm WebGraph the posting list of the node 16, with respect to the one of node 15:

$$
\begin{aligned}
& 15->~ 1,3,5,6,7,8,10,16,17,22,24,44 \\
& 16->2,3,5,6,7,8,9,10,16,17,20,21,22,24
\end{aligned}
$$

Question \#2 [scores 3+4] You are given three sets $A=\{2,5,6,9\}, B=\{1,2,4\}$ and $C=\{1,5,6,9\}$.

- Compute the Jaccard similarity between all pairs of them
- Approximate the Jaccard similarity via Min-Hashing, by using the following three permutations: $\pi_{1}(x)=3 * x \bmod 11, \pi_{2}(x)=x+5 \bmod 11, \pi_{3}(x)=4 * x \bmod 11$

Question \#3 [scores 4] Given the dictionary of strings $D=\{A A B, A B A, A C A\}$ construct a bigram index (hence $k=2$ ). Then given the string $Q=$ "BAAB" use the overlap distance to filter a set of strings from $D$ that are potential candidate for an edit distance $\mathrm{e}=1$.

Question \#4 [scores 3+1] Consider the Blocked-WAND algorithm for examining the head of the following four posting lists:

$$
\begin{aligned}
& \mathrm{t}_{1} \rightarrow 7,9,10,11,14 \\
& \mathrm{t}_{2} \rightarrow 3,4,6,7,8,10,11,14,16,19 \\
& \mathrm{t}_{3} \rightarrow 6,7,8,10,15 \\
& \mathrm{t}_{4} \rightarrow 1,3,6,8,9,11,13,14,15,16
\end{aligned}
$$

The current threshold is $\theta=2.8$, the upper bounds of the scores in each posting list are: $u_{1}=2$, $u b_{2}=1.5, u b_{3}=0.5, u b_{4}=1$, the blocks are of size 5 , and the local upper bounds of the first block in each list are equal to $\mathrm{lb}_{1}=2, \mathrm{lb}_{2}=1, \mathrm{lb}_{3}=0.5, \mathrm{lb}_{4}=1$.
a) Which is the candidate docID, and is its full score computed?
b) Show the docID pointed by each iterator at the end of the Blocked-WAND step (that is, just before determining the next candidate docID).

Question \#5 [scores 3] Compute one step of PageRank on the following graph by assuming $\alpha=1 / 2$ and the starting probability distribution $r(A)=2 / 4, r(B)=1 / 4, r(C)=0, r(D)=1 / 4$.


# Information Retrieval - THEORY 

## 16 January 2024 - time 45 minutes

## Name and Surname:

## \#matricola:

Question \#1 [scores 4] Describe the two approaches to dynamic indexing: i.e., 2 indexes and a cascade of indexes; and comment on the time complexity of inserting one document, by assuming that the collection consists of $N$ documents (all of the same size, for simplicity) and the machine consists of an internal memory of size M.

Question \#2 [scores 2] What are the minimum and maximum number of integers that Simple9 can encode in a single 32-bit word, and why?

Question \#3 [scores 2] Describe the champion lists approach for approximate top-K retrieval.

