

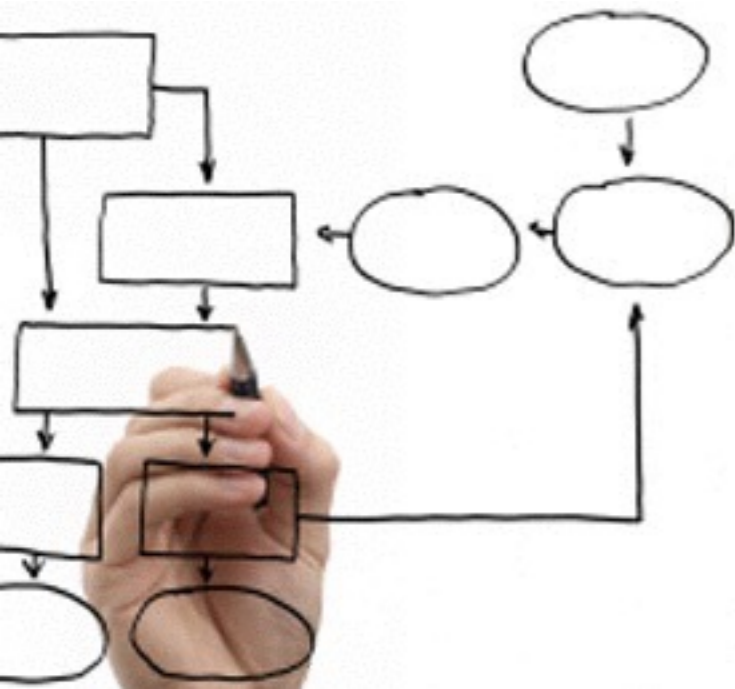
# Methods for the specification and verification of business processes

MPB (6 cfu, 295AA)

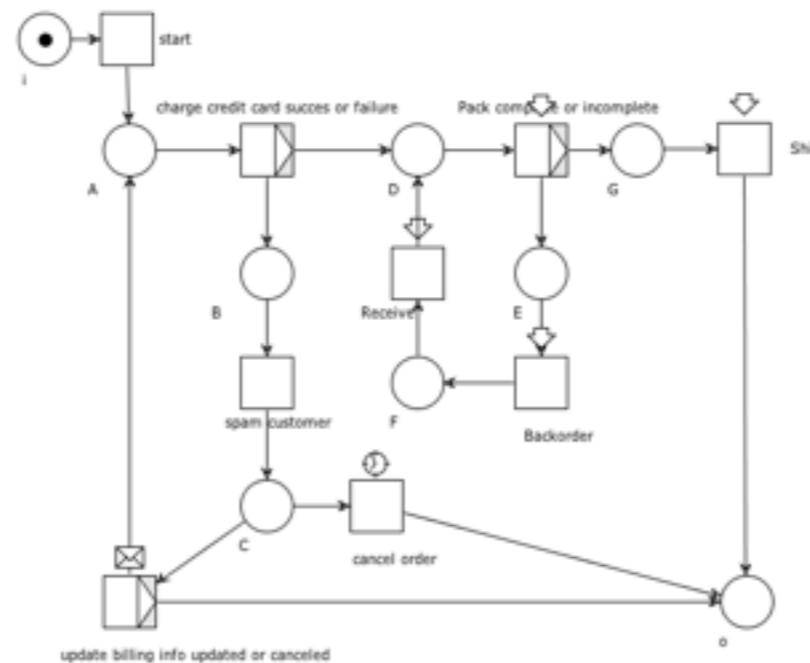
Roberto Bruni

<http://www.di.unipi.it/~bruni>

12 - Workflow nets



# Object



We study some special kind of Petri nets,  
that are suitable models of workflows

There are many, many  
variants of Petri nets

# Condition / Event Systems

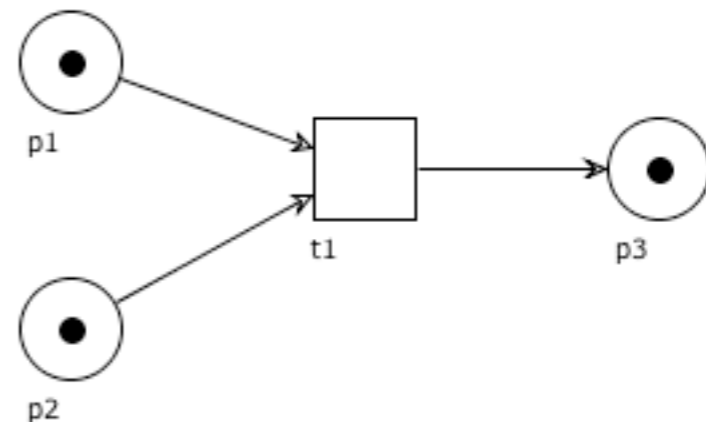
A **C/E system** is a Petri net whose places have all capacity equal to 1  
(i.e., each place can contain one token at most)

Markings are just subsets of  $P$  (not multisets)

Firing rule is more restrictive:

$t$  is enabled at  $M$  if  $\bullet t \subseteq M$  and  $t \bullet \cap M = \emptyset$

Is  $t_1$  enabled?



# Place / Transition Petri nets

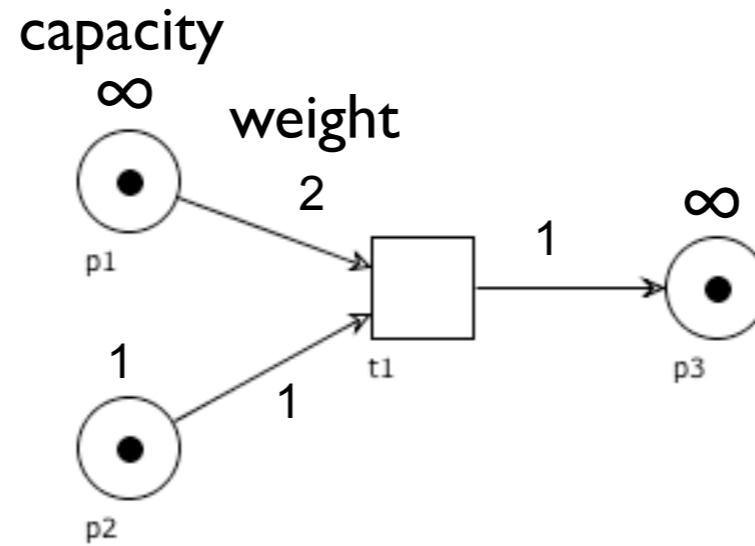
A **P/T net** is a Petri net  $(P, T, F)$  together with a weight function  $w : F \rightarrow \text{Nat}$

Firings consume and produce tokens according to the weight function

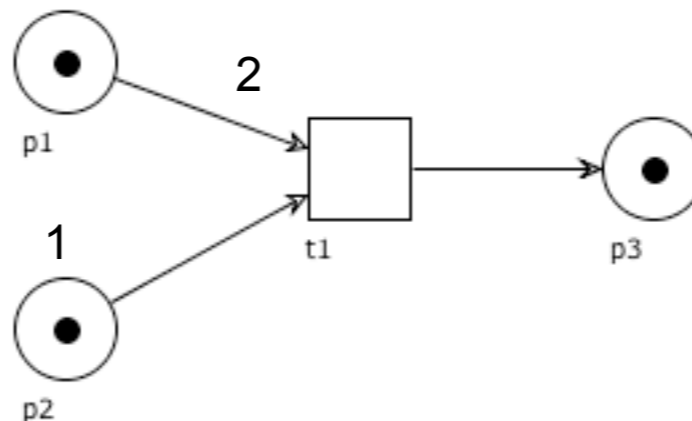
Sometimes a place capacity function  $c : P \rightarrow \text{Nat} \cup \{\infty\}$  is also considered

Firings cannot lead to markings where the capacity of a place is exceeded

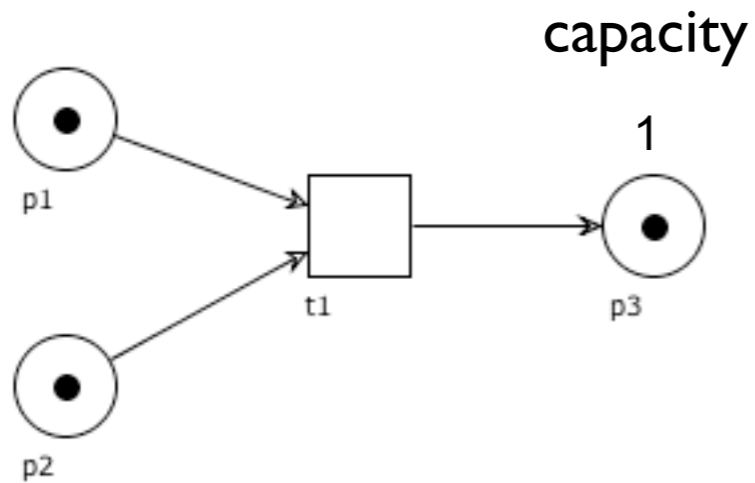
# P/T net: examples



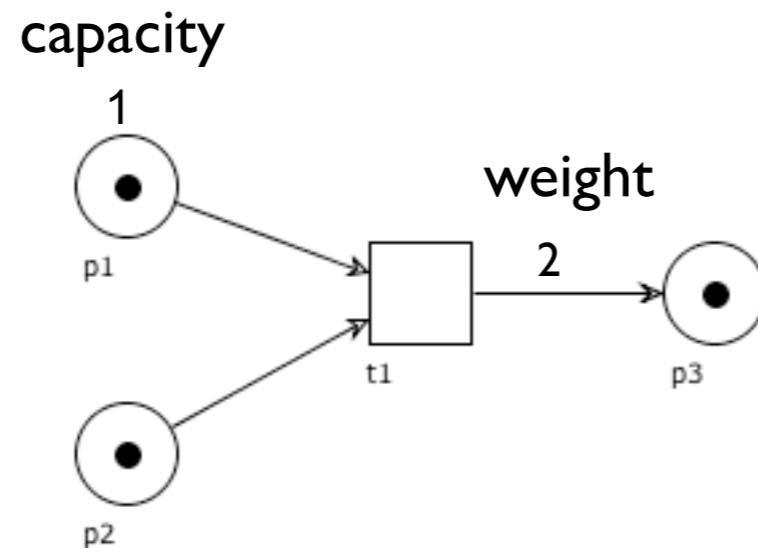
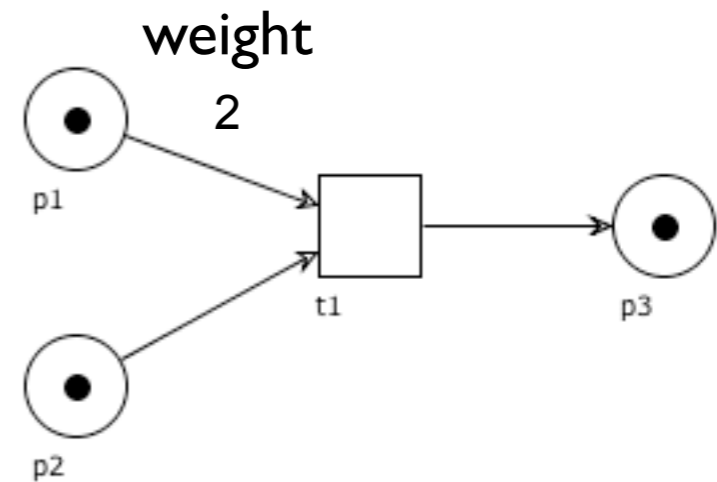
Capacity  $\infty$  is omitted from places  
Weight 1 is omitted from arcs



# P/T net: examples



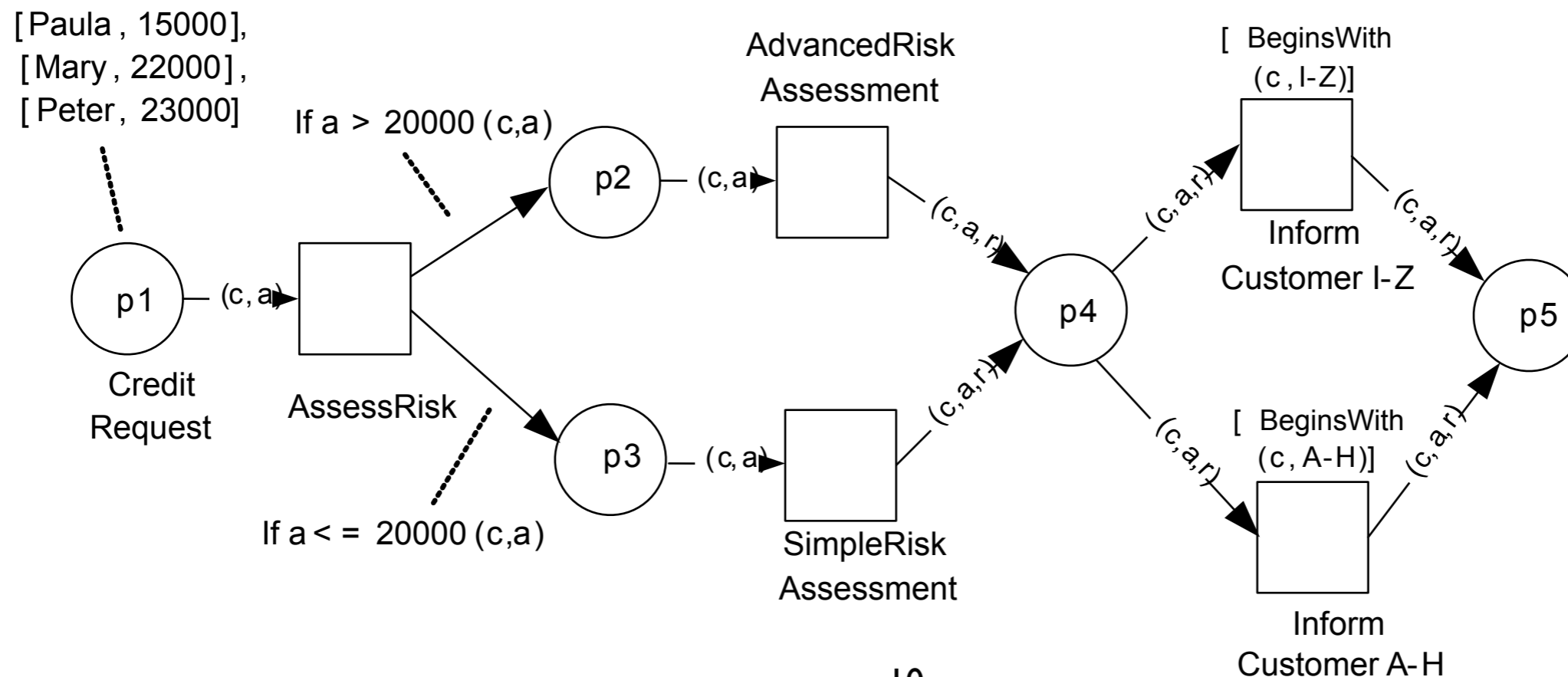
Is  $t_1$  enabled?



# Coloured nets

## (also called High-Level)

A **coloured net** is a Petri net whose tokens can carry data and whose transitions can check data (see exact definition in Weske's book)





# Workflow nets

# Workflow nets features

**Aim:** To ease the representation of business processes

Formal (unambiguous) semantics

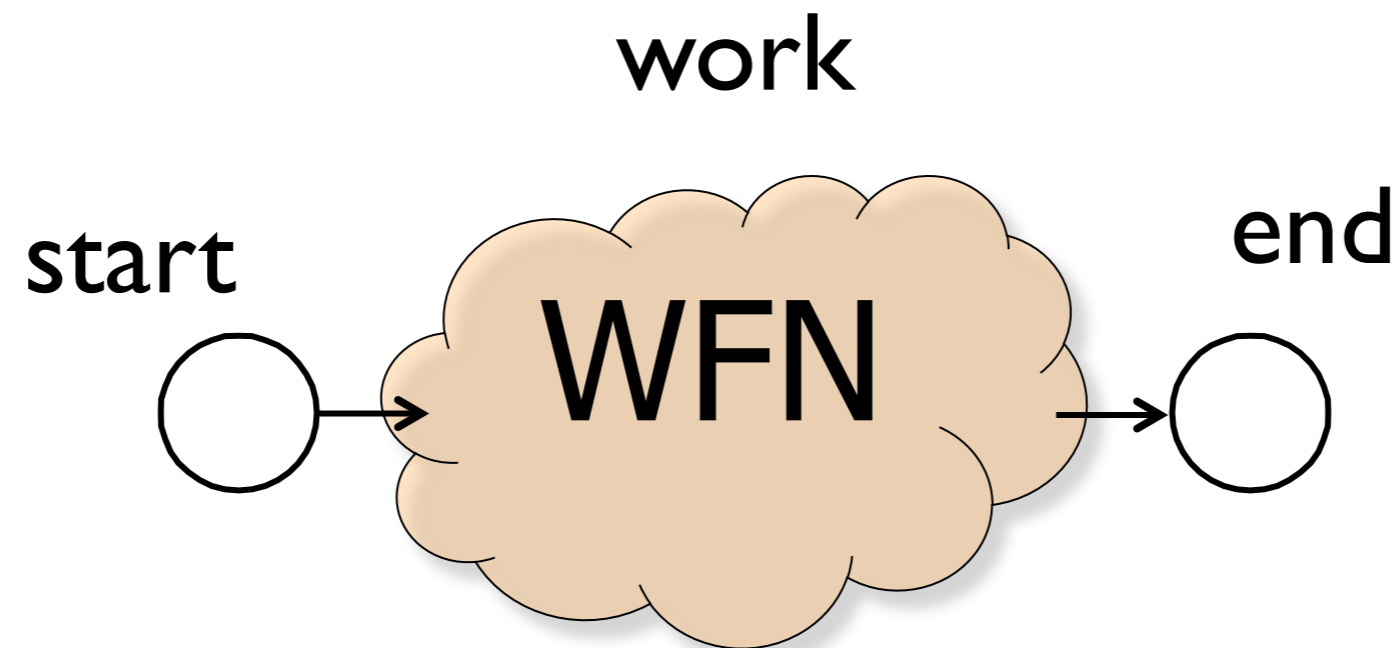
Decorated graphical representation

Structural restrictions

Efficient analysis of process properties

Tool independence (.pnml standard)

# Workflow net: idea



# Workflow net

## Definition:

A Petri net  $(P, T, F)$  is called **workflow net** if:

1. there is a distinguished *initial place*  $i \in P$  with  $\bullet i = \emptyset$
2. there is a distinguished *final place*  $o \in P$  with  $o \bullet = \emptyset$
3. every other place and transition belongs to a path from  $i$  to  $o$

# Workflow net: Rationale

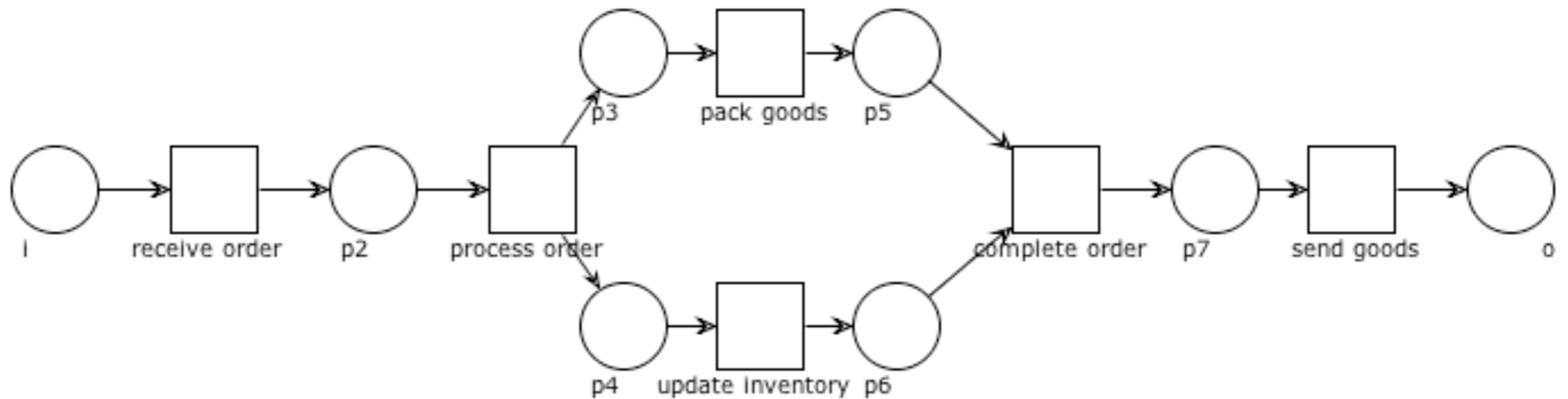
1. a token in  $i$  represents a process instance not yet started
2. a token in  $o$  represents a finished case
3. each place and each transition can participate in a case

## Definition:

A Petri net  $(P, T, F)$  is called **workflow net** if:

1. there is a distinguished *initial place*  $i \in P$  with  $\bullet i = \emptyset$
2. there is a distinguished *final place*  $o \in P$  with  $o \bullet = \emptyset$
3. every other place and transition belongs to a path from  $i$  to  $o$

# WF net: Example



# Basic properties

**Lemma:** In a workflow net there is a **unique** node with no incoming arc

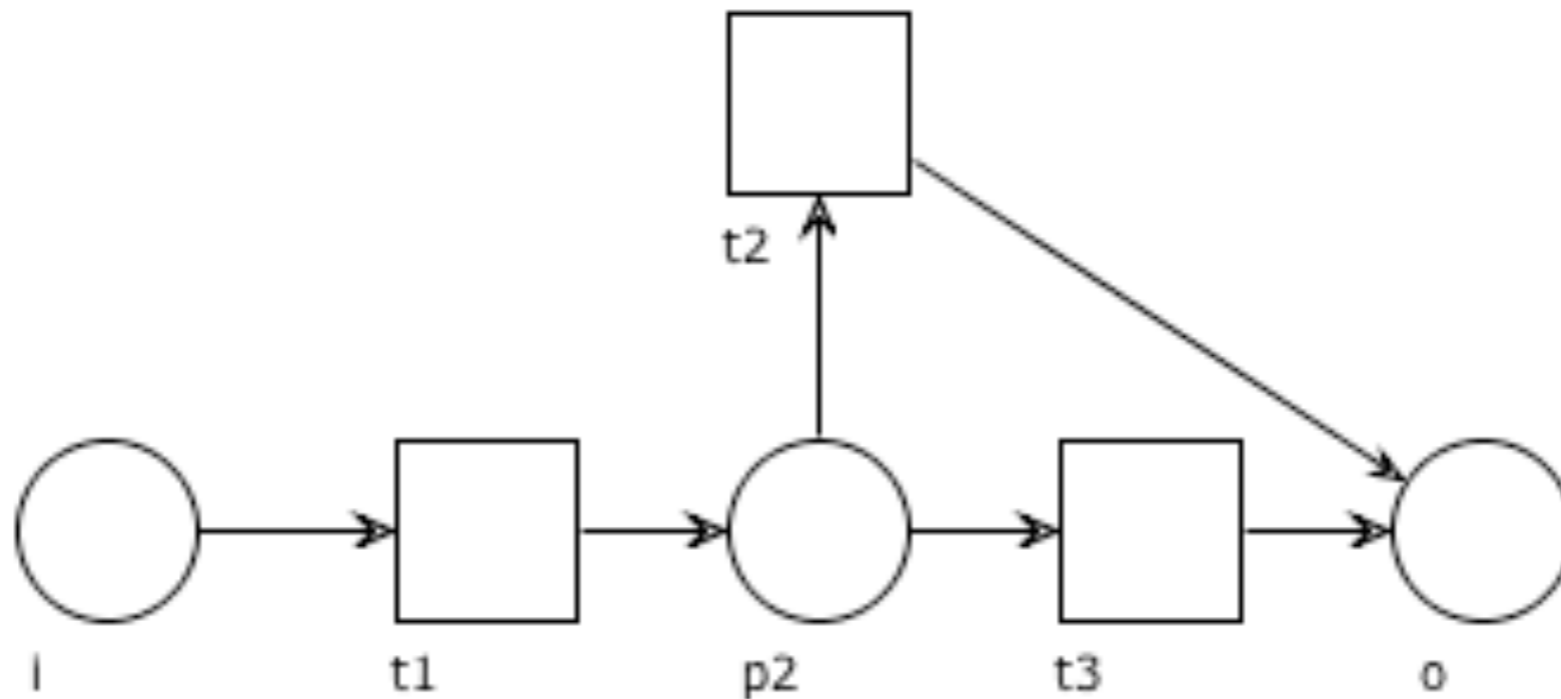
**Lemma:** In a workflow net there is a **unique** node with no outgoing arc

**Exercise:** Guess which nodes are those

**Exercise:** Prove the above lemmas

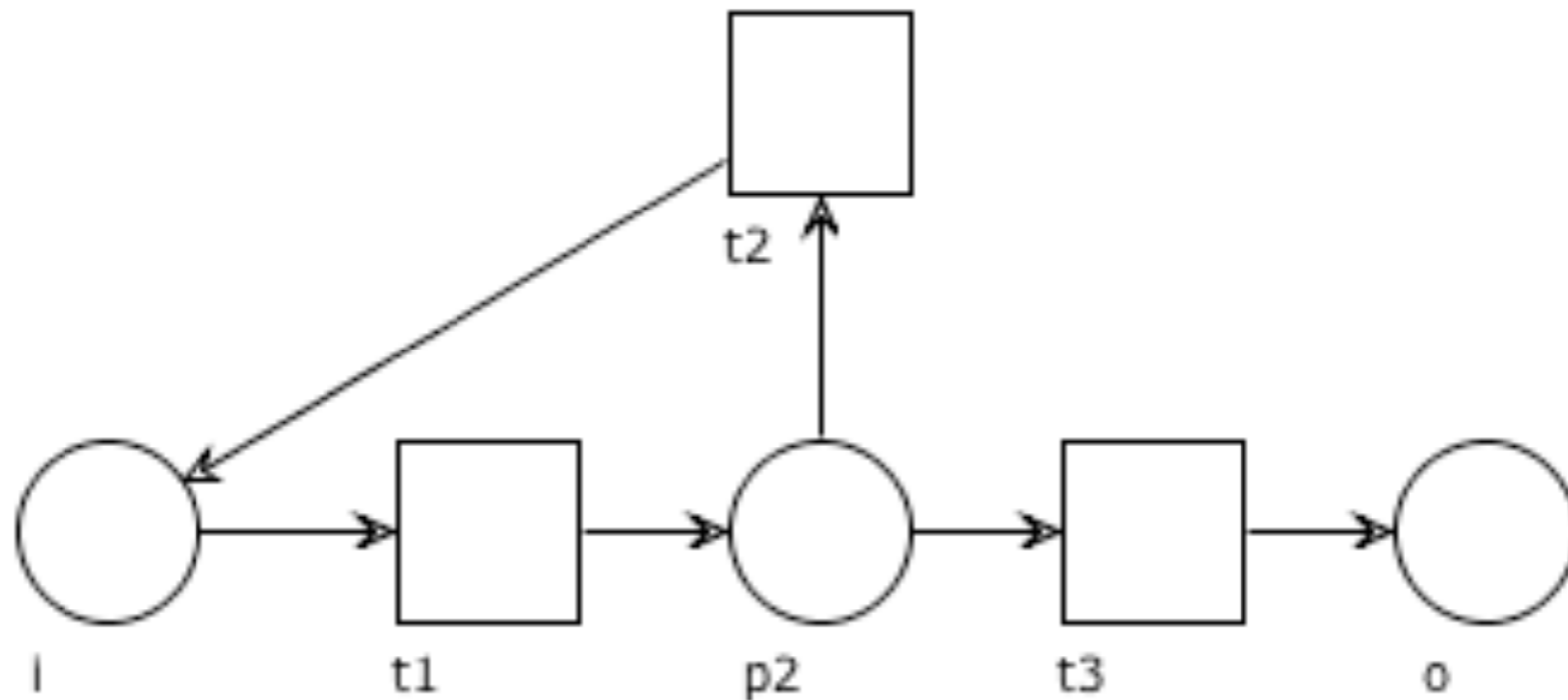
(hint: suppose the nodes are not unique, reach a contradiction)

# Question time: WF net?

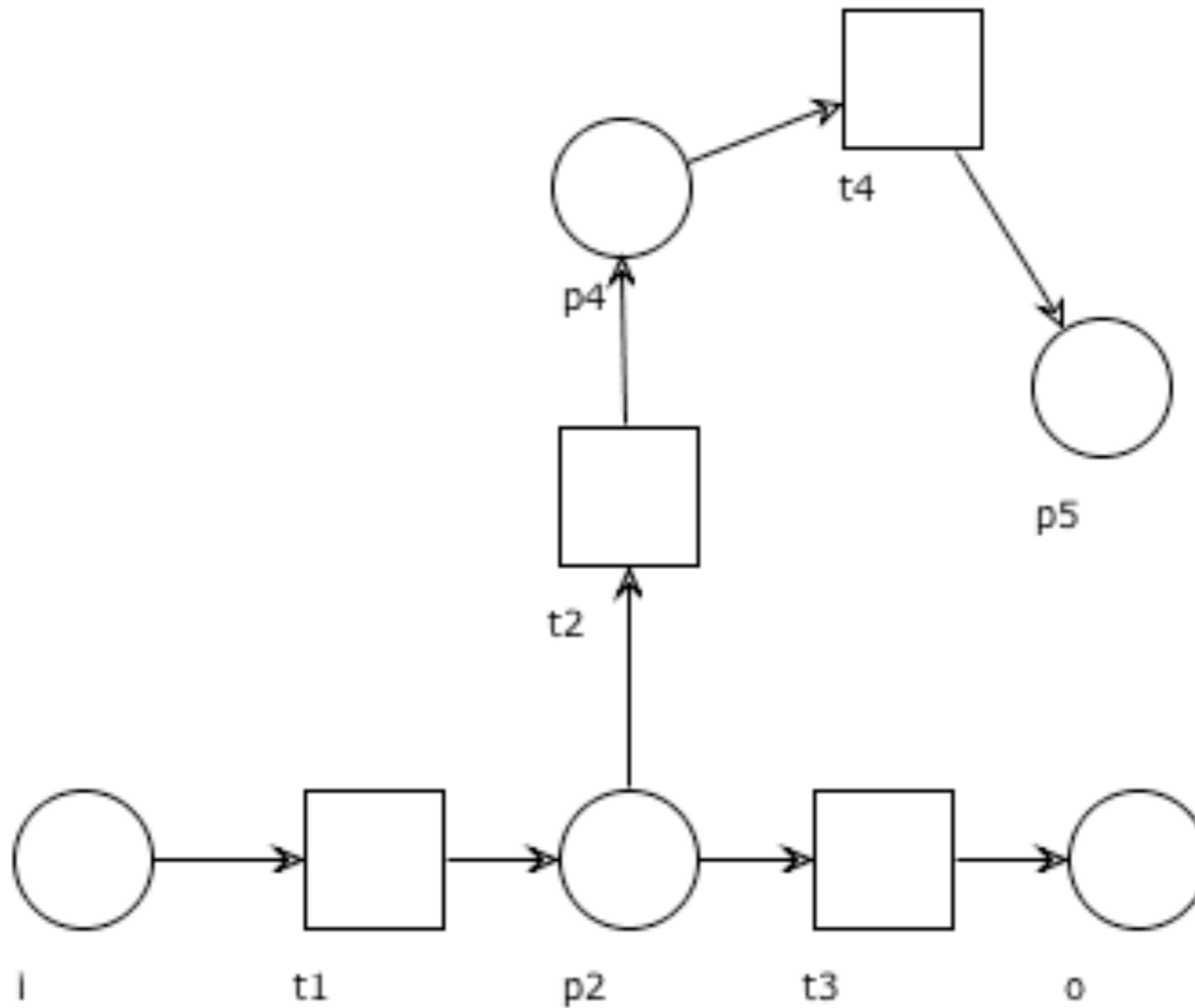




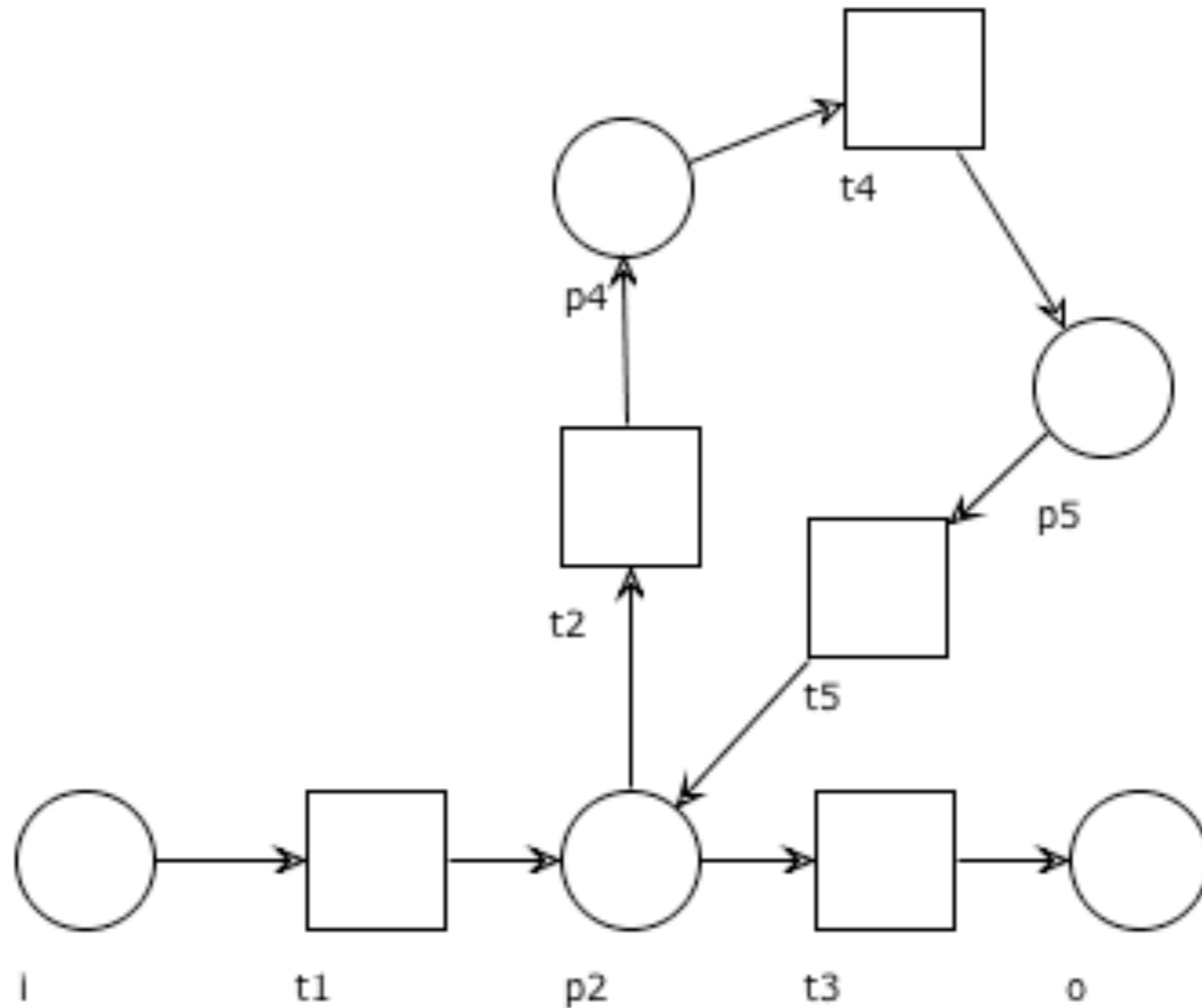
# Question time: WF net?



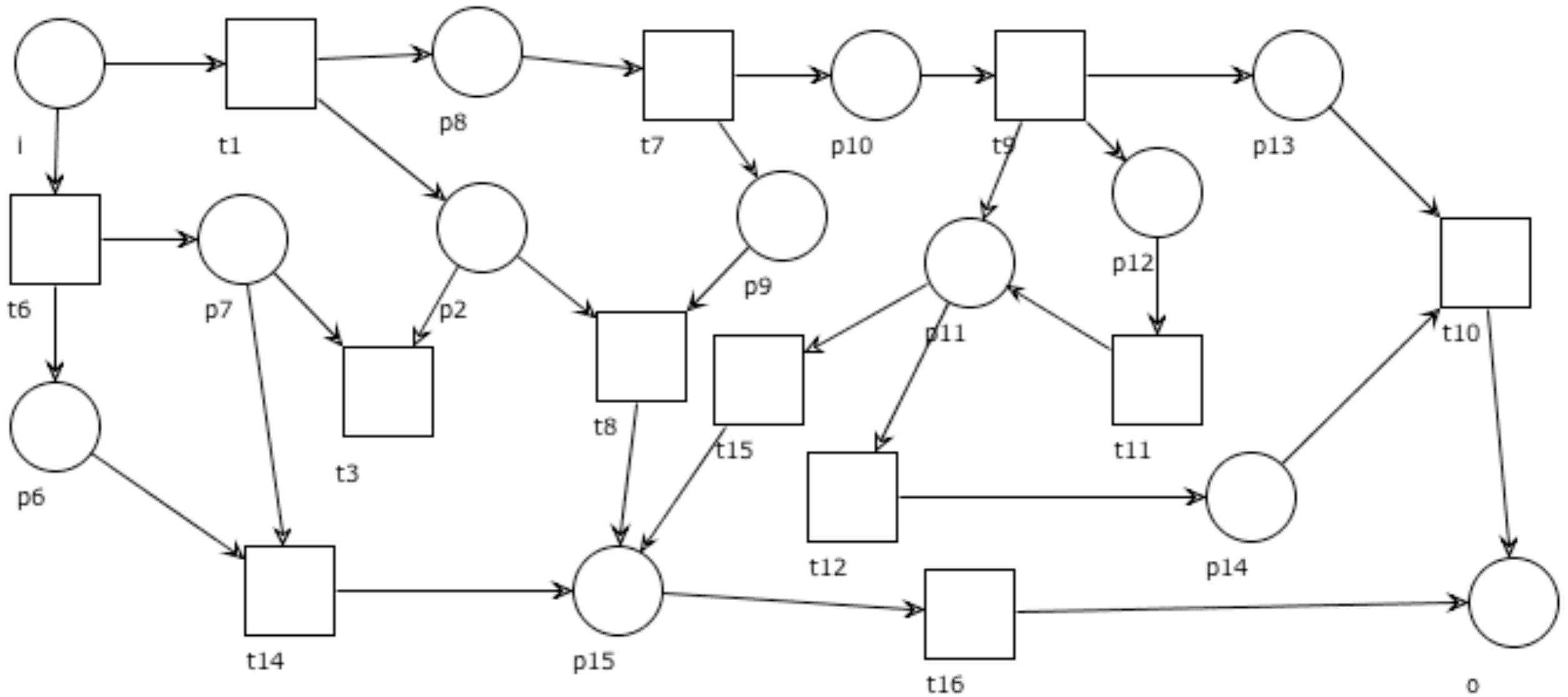
# Question time: WF net?



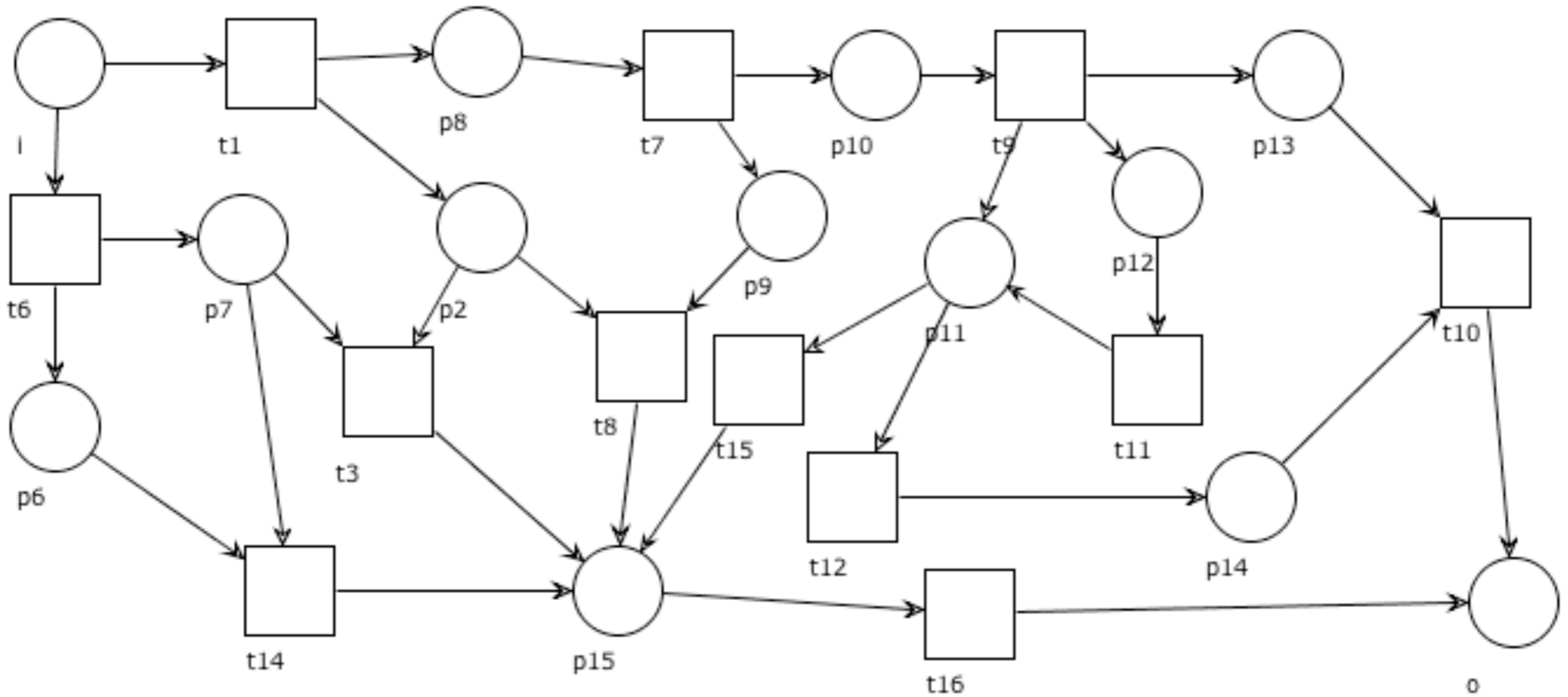
# Question time: WF net?



# Question time: WF net?

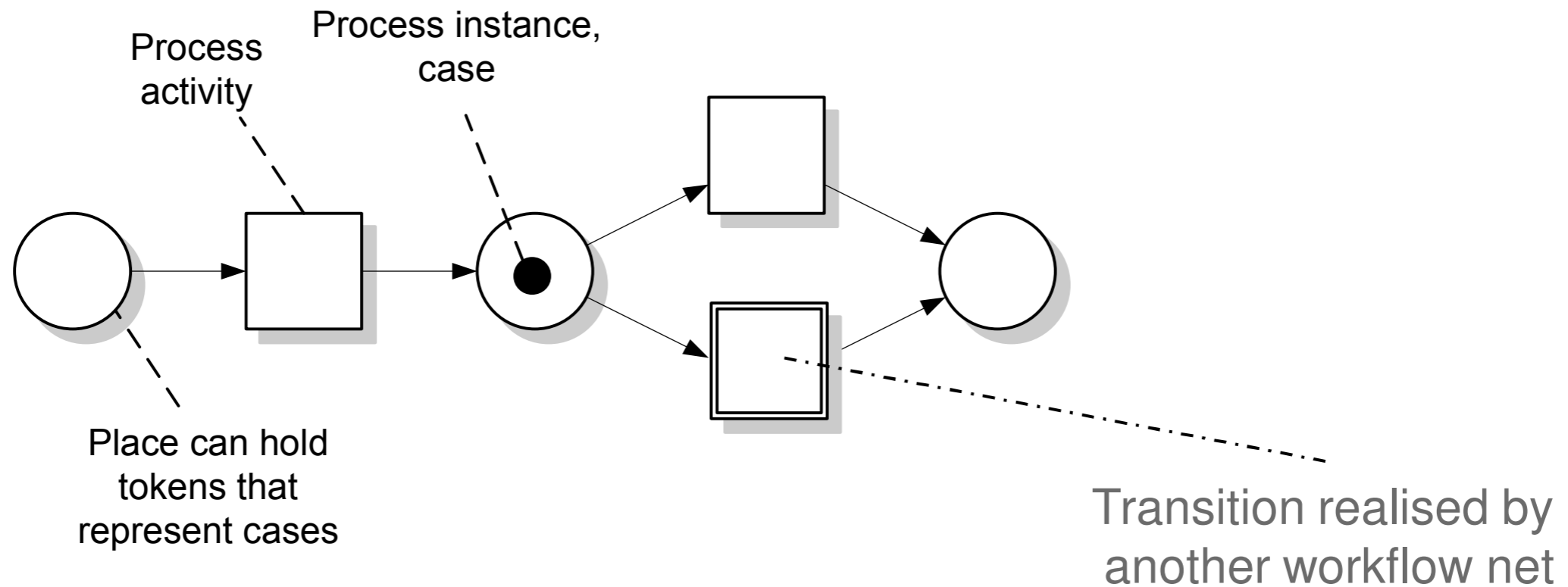


# Question time: WF net?

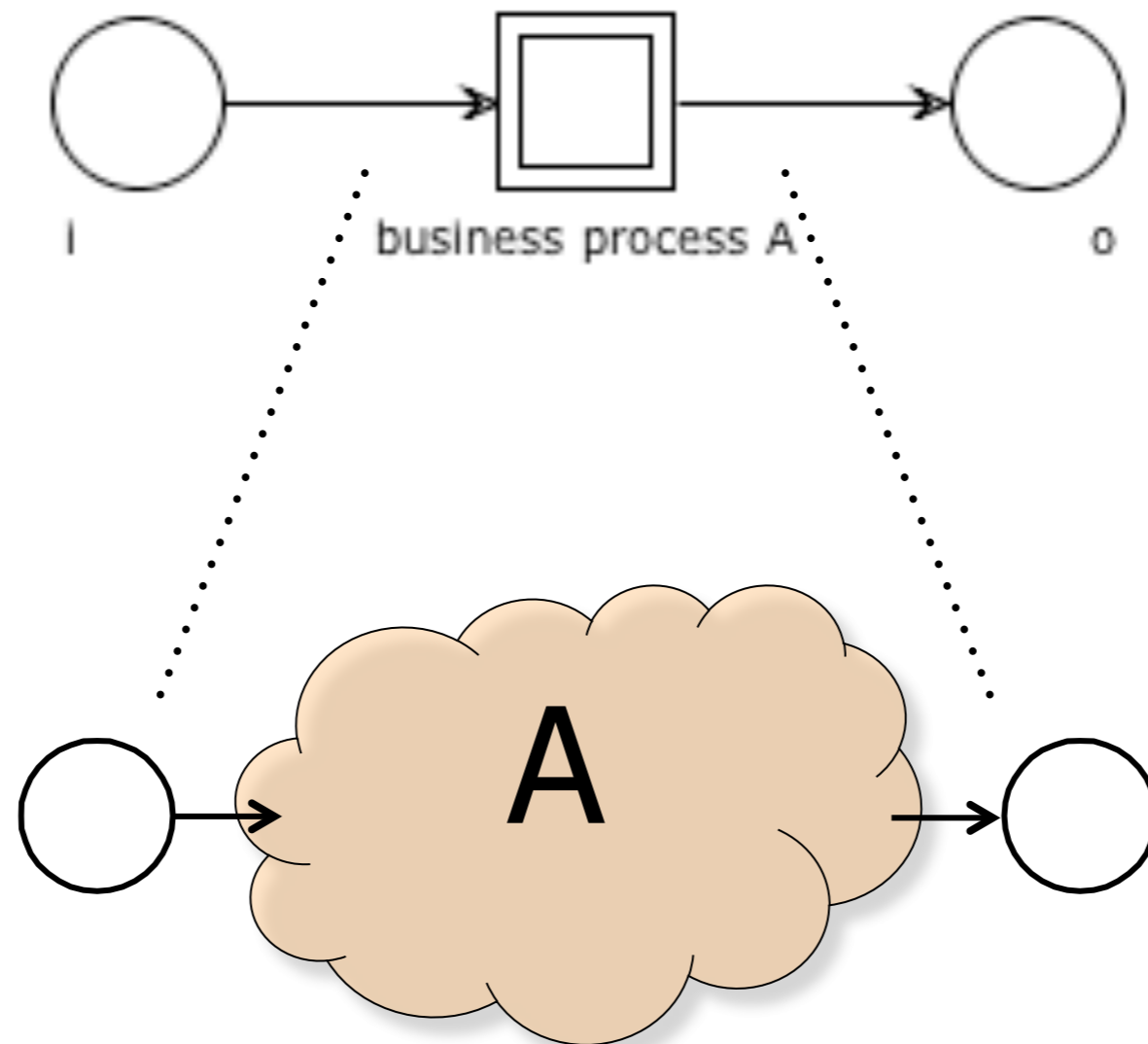


# Hierarchical structuring

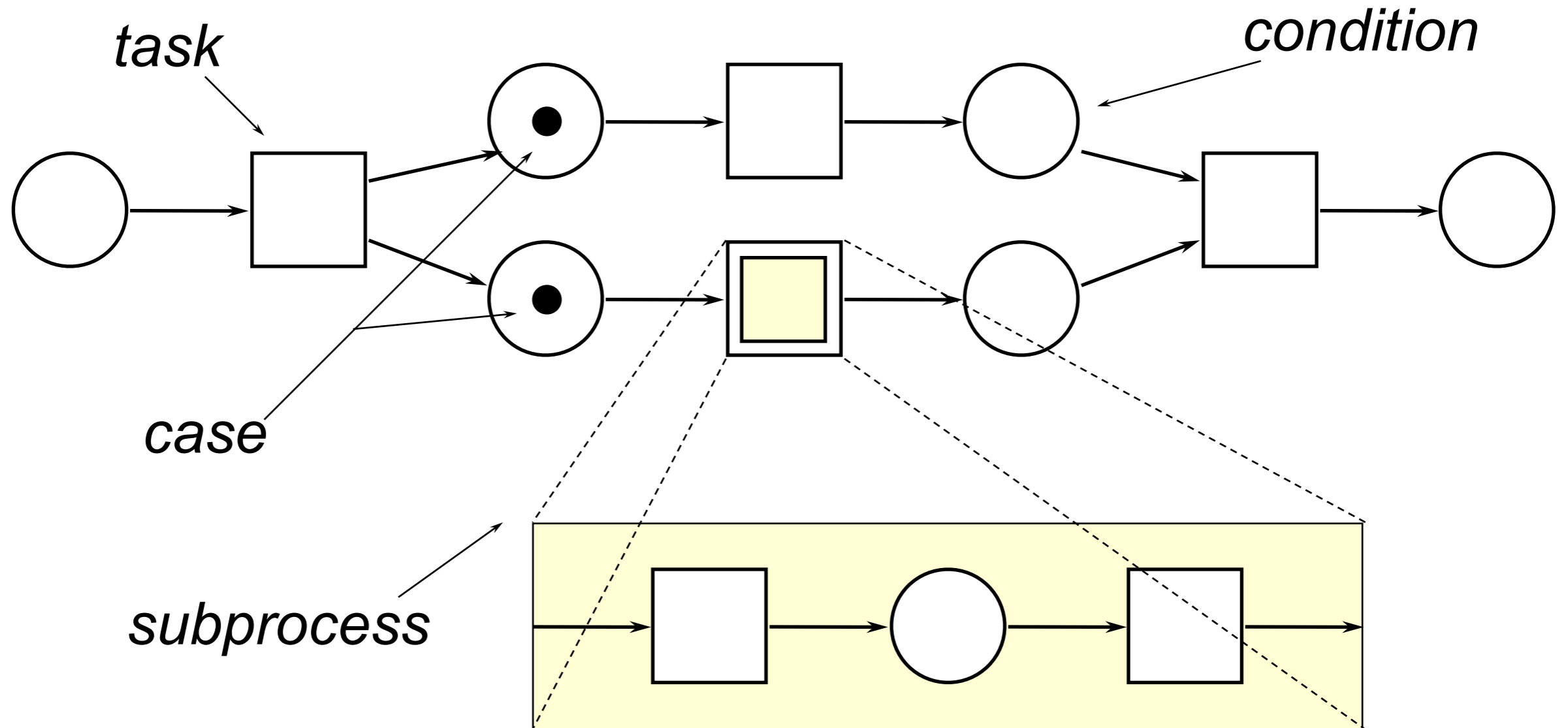
Uniqueness of entry / exit point facilitate the hierarchical structuring of WF nets



# Abstract view



# Subprocesses





# Typical control flow aspects

Sequencing

Parallelism (AND-split + AND-join)

Selection (XOR-split + XOR-join)

Iteration (XOR-join + XOR-split)

Capacity constraints:

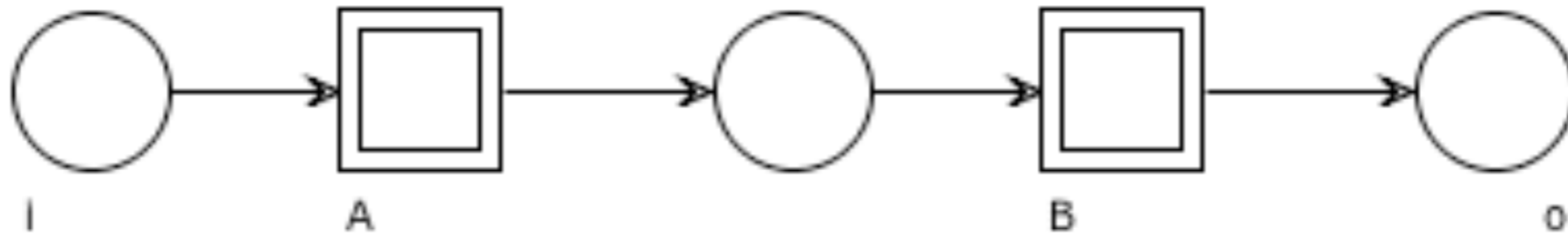
Feedback loop

Mutual exclusion

Alternating

# Sequencing

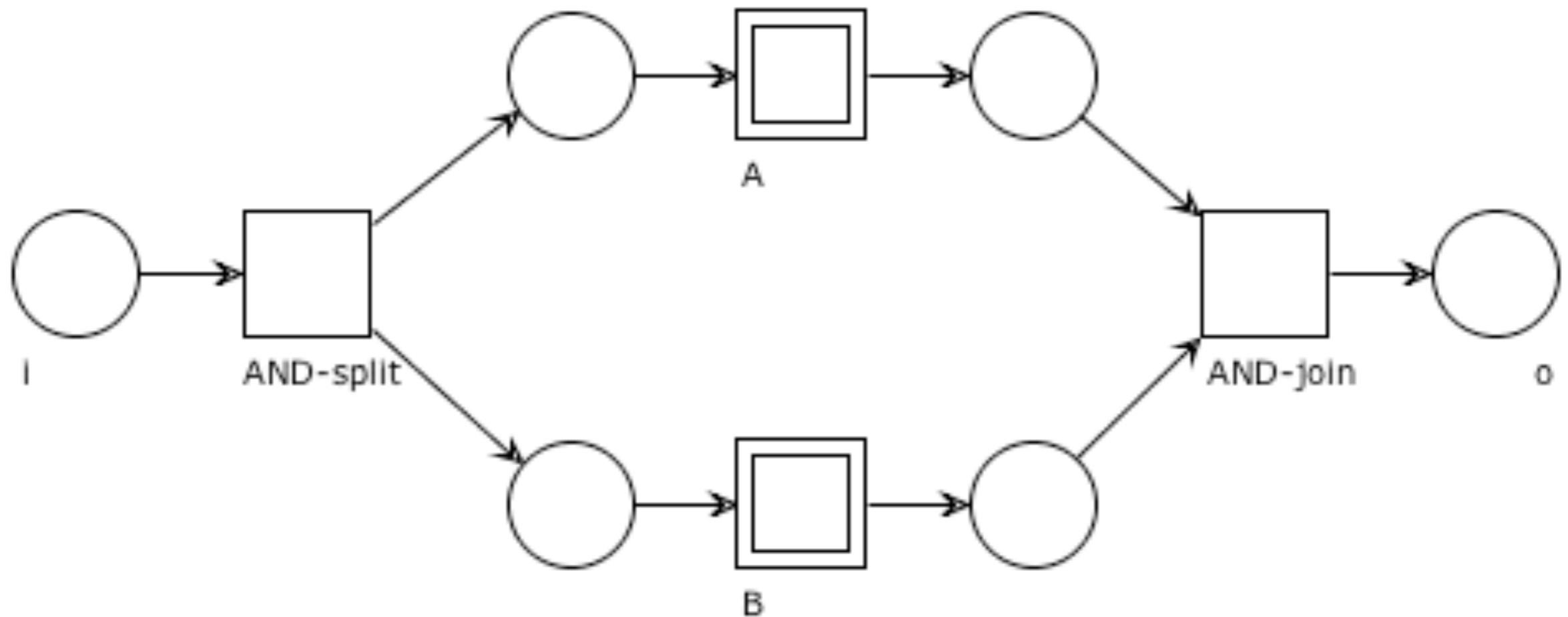
B is executed after A



# Parallelism

(AND-split + AND-join)

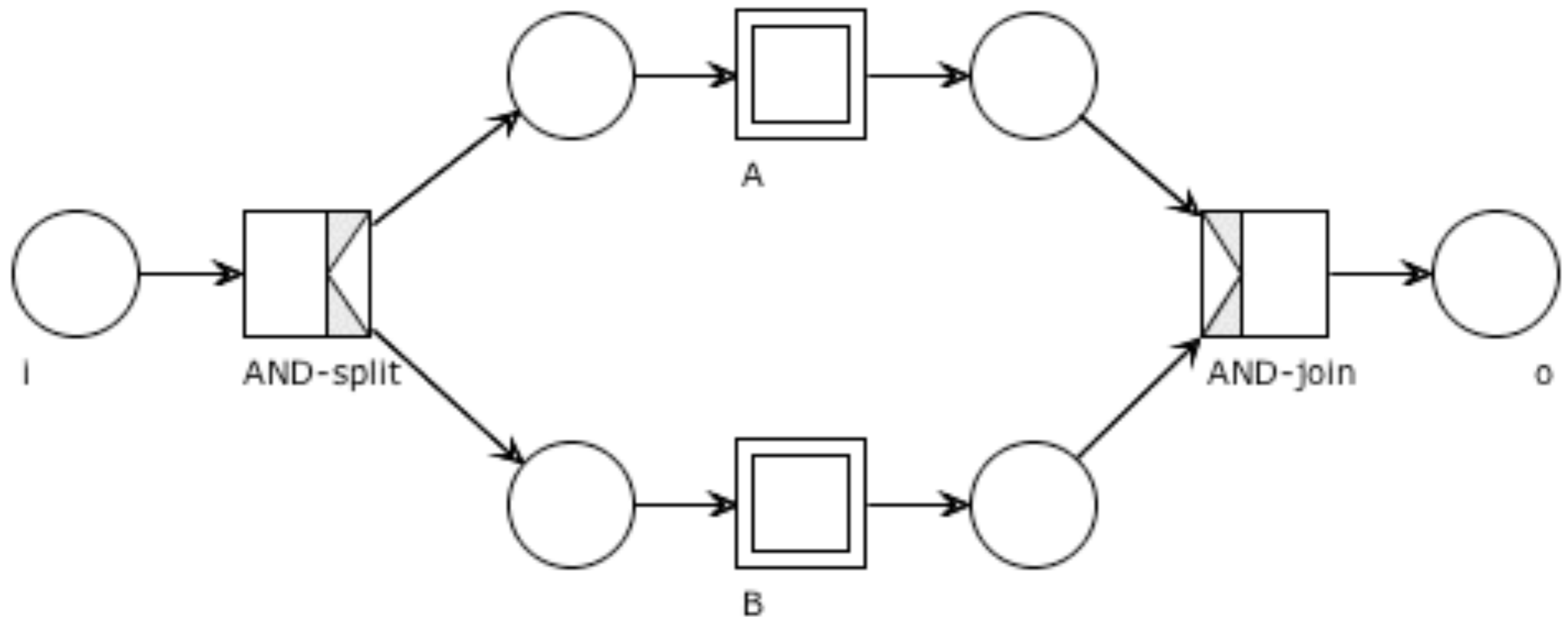
A and B are both executed in no particular order



# Parallelism

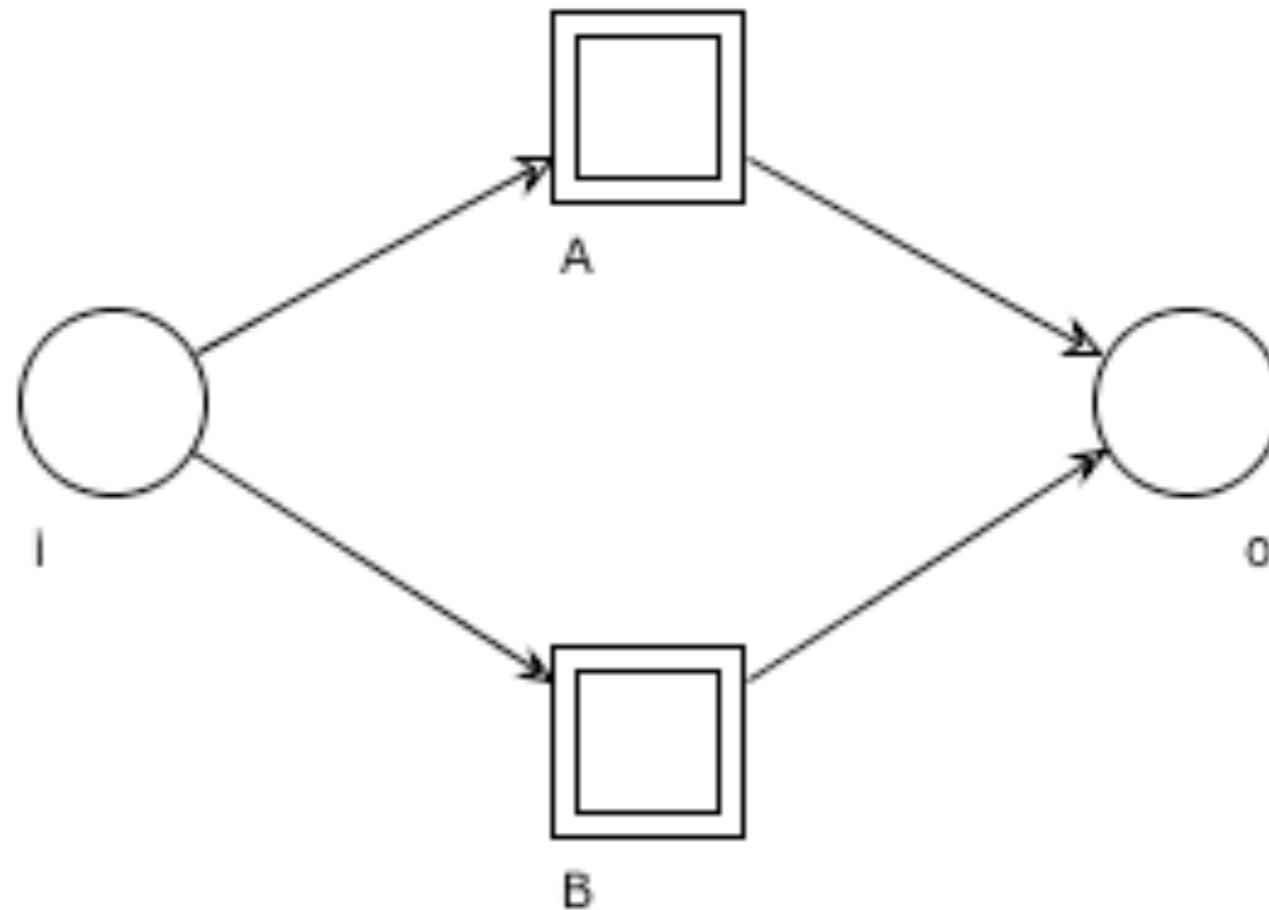
## ("sugared" version)

Decorated version for business process stakeholders



# Deferred choice (XOR-split + XOR-join)

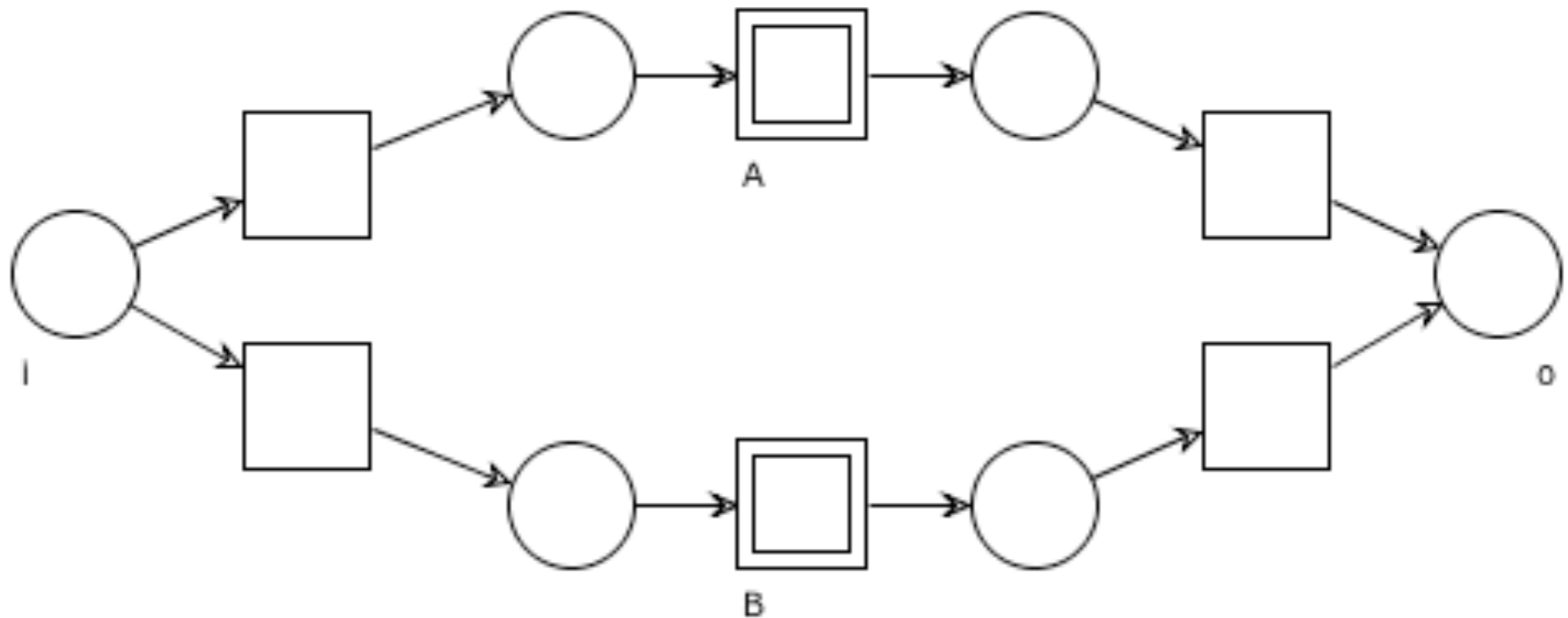
Either A or B is executed (choice is **implicit**)



# Explicit choice

(XOR-split + XOR-join)

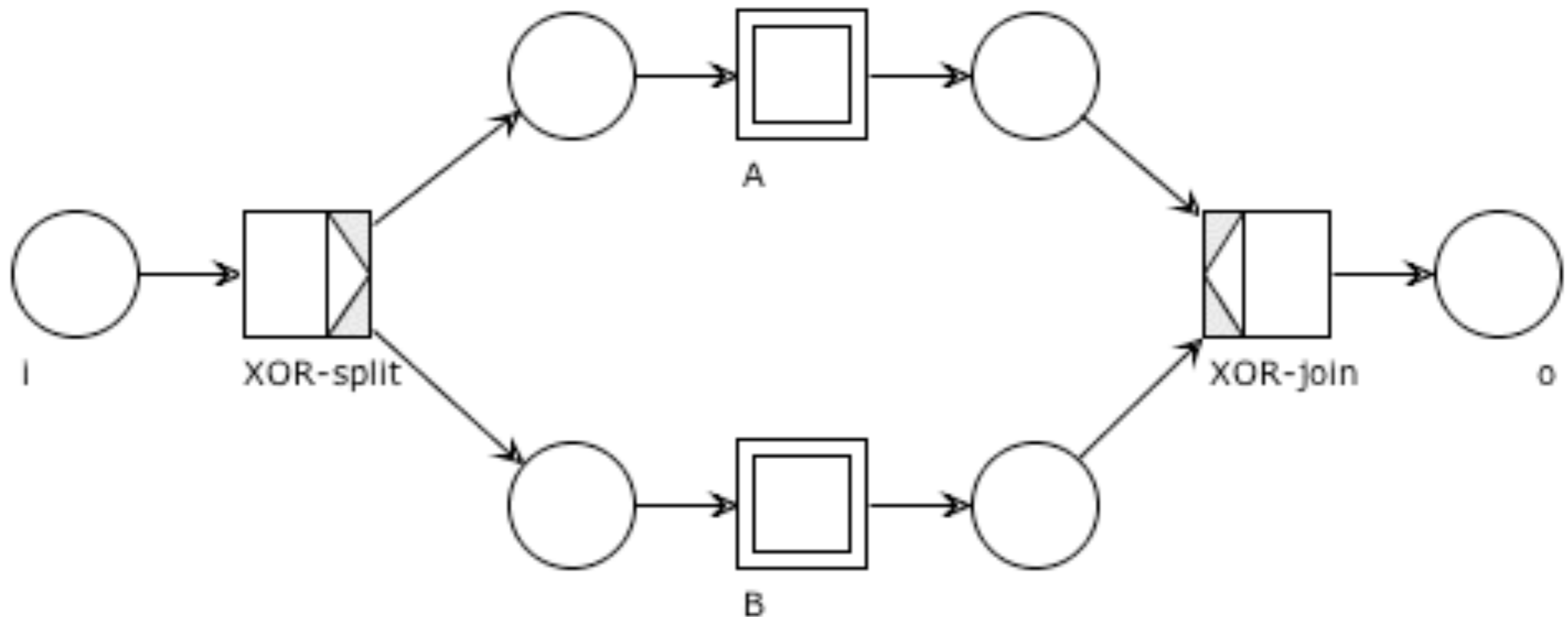
Either A or B is executed (choice is **explicit**)



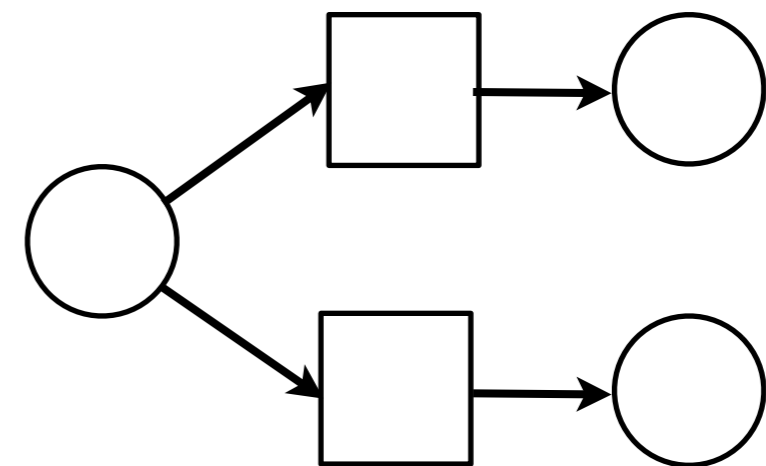
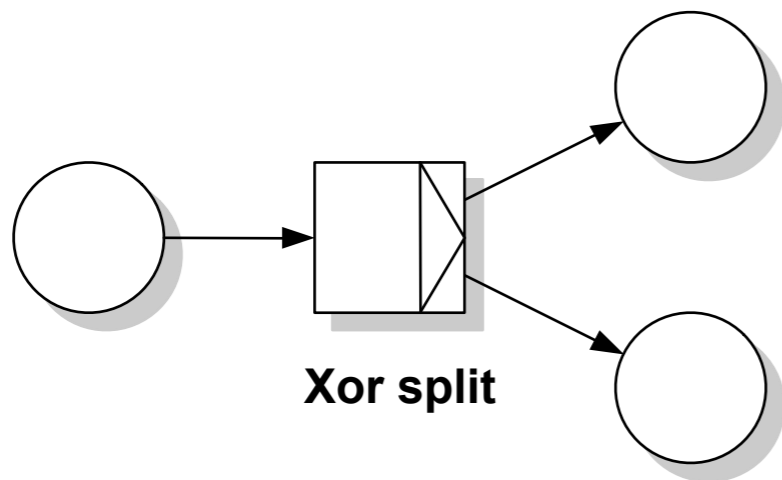
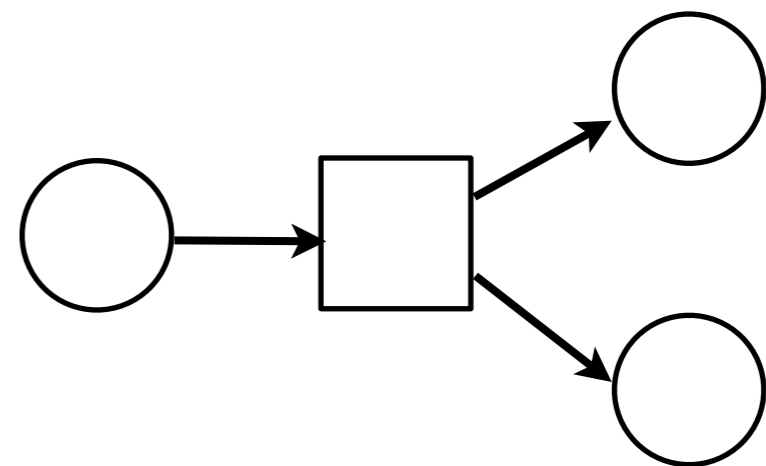
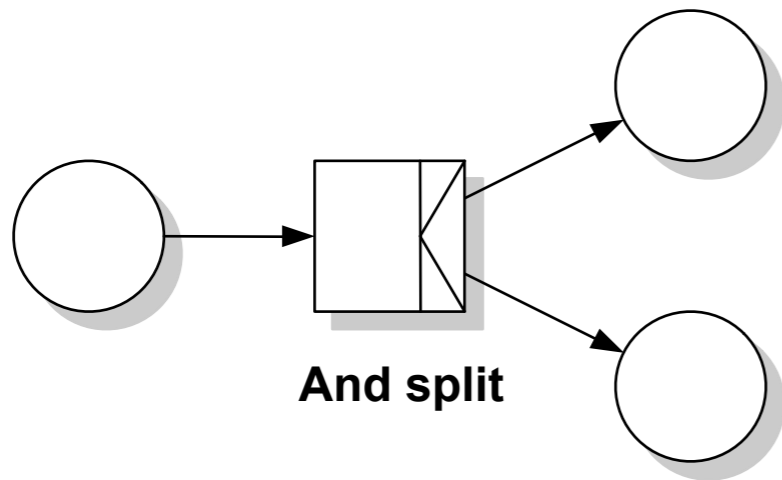
# Choice

## ("sugared" version)

Decorated version for business process stakeholders



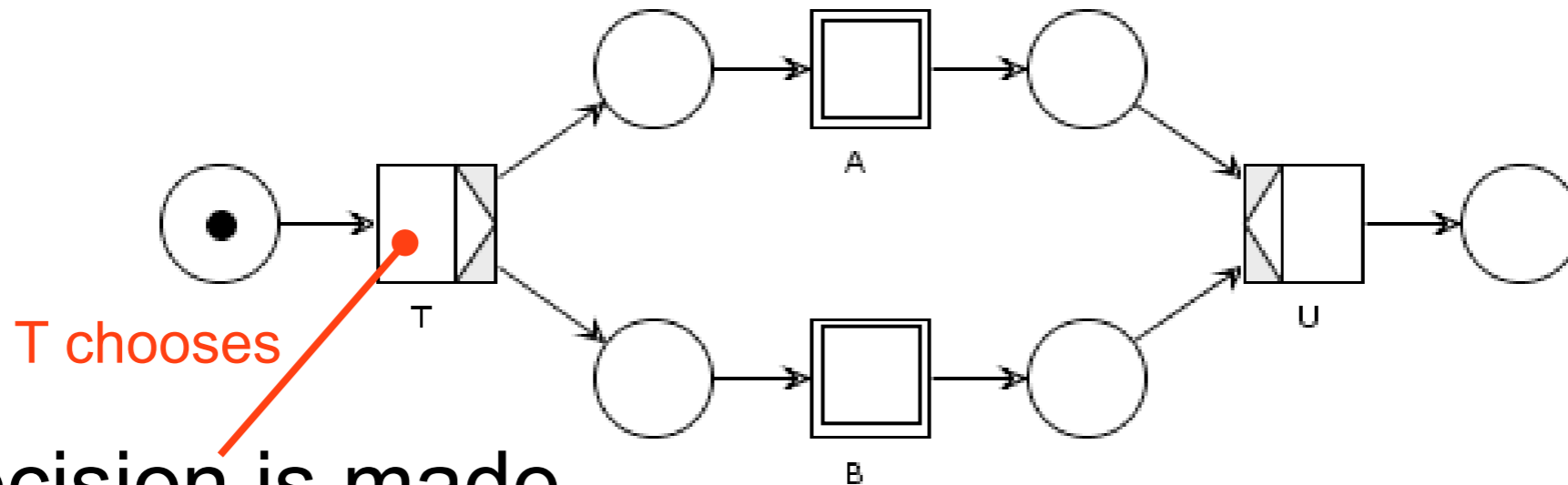
# Syntax Sugar



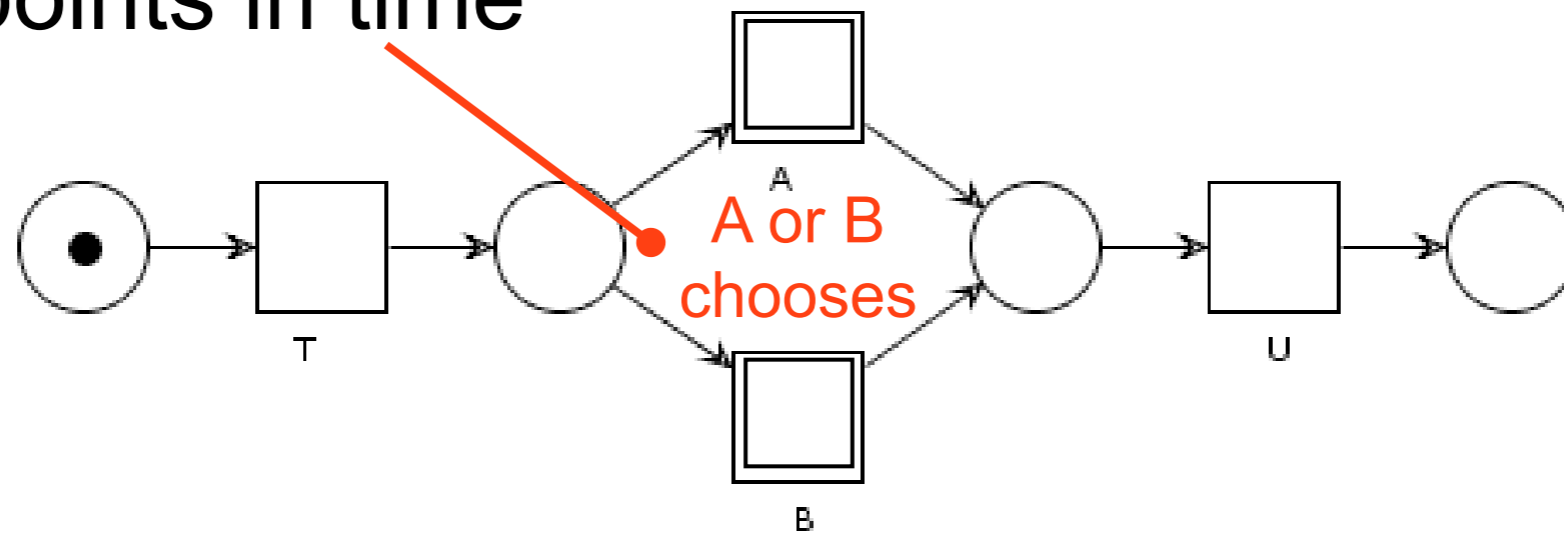


# Remember

Explicit choice  $\neq$  Implicit choice

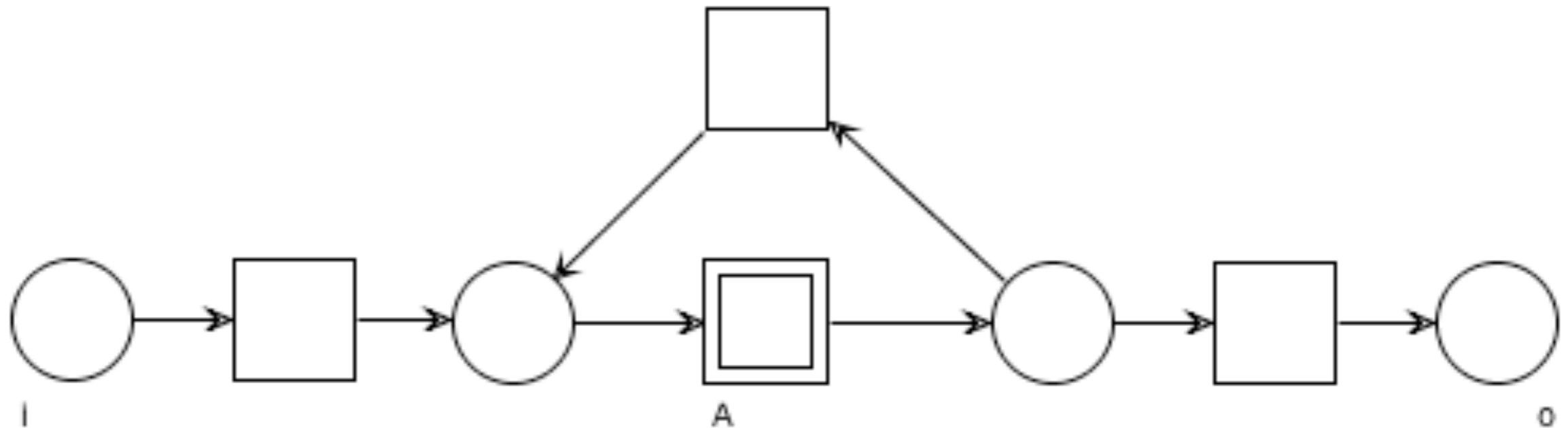


The decision is made at different points in time



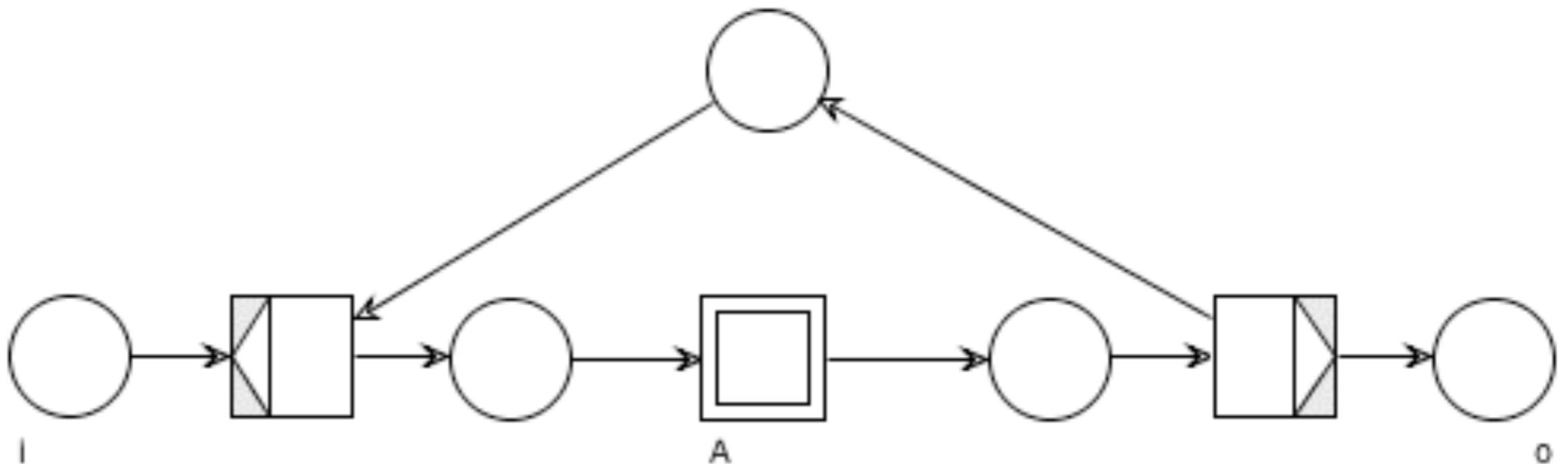
# Iteration (one or more time)

A is executed 1 or more time



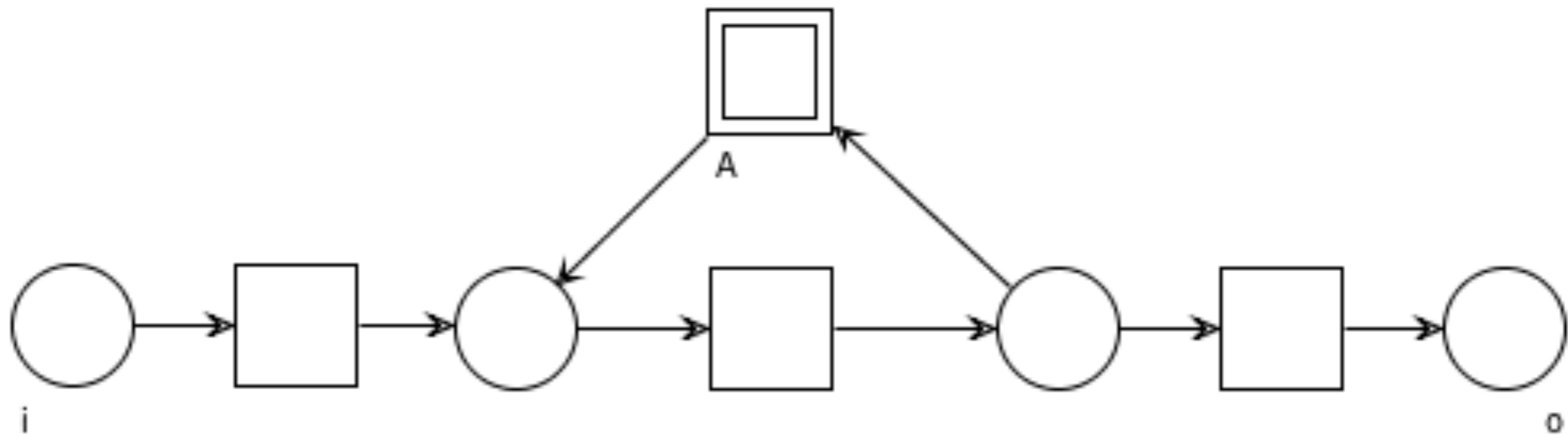
# One-or-more iteration ("sugared" version)

Decorated version for business process stakeholders



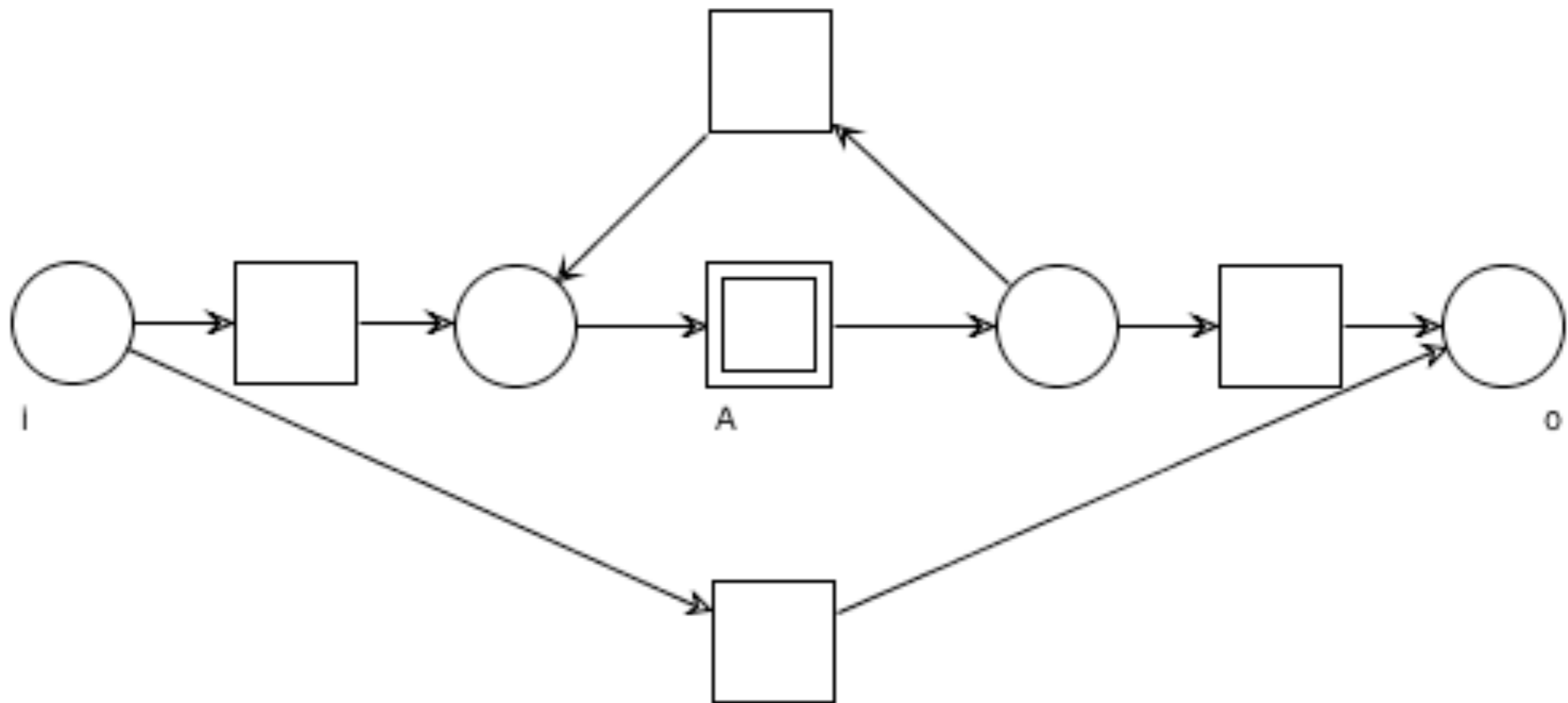
# Iteration (zero or more time)

A is executed 0 or more time



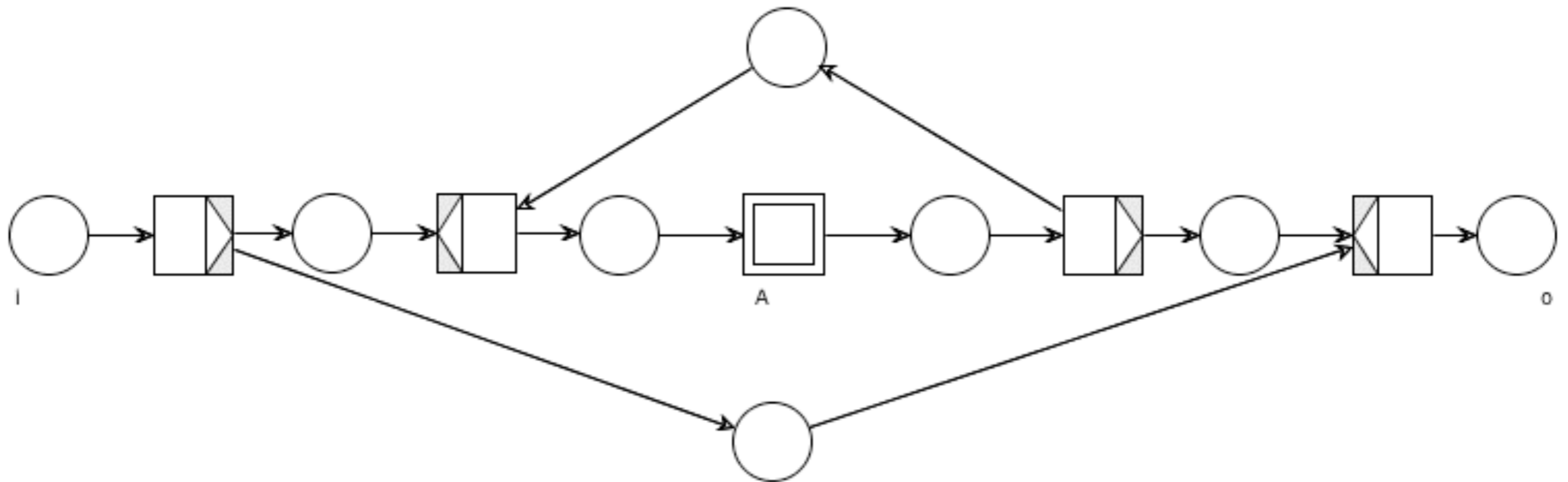
# Iteration (zero or more time)

A is executed 0 or more time



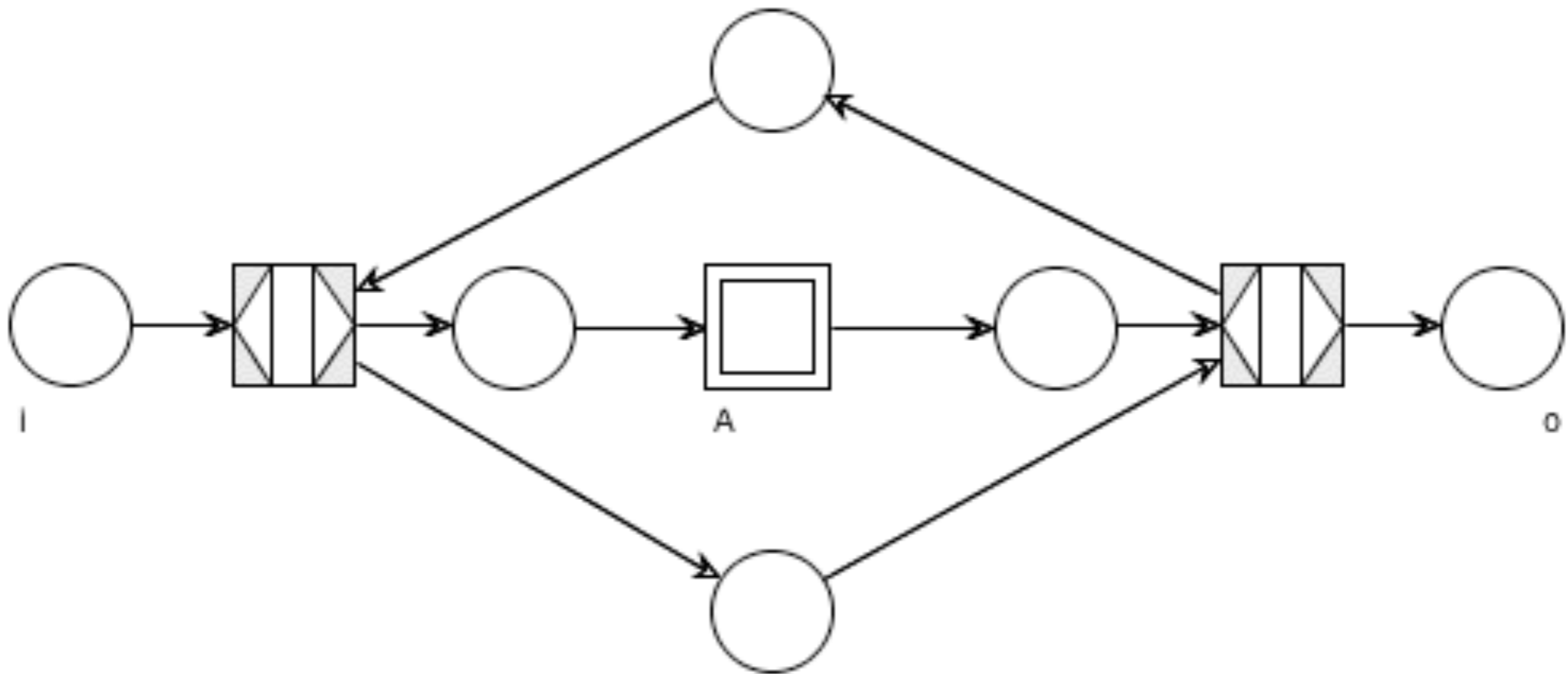
# Zero-or-more iteration ("sugared" version)

Decorated version for business process stakeholders



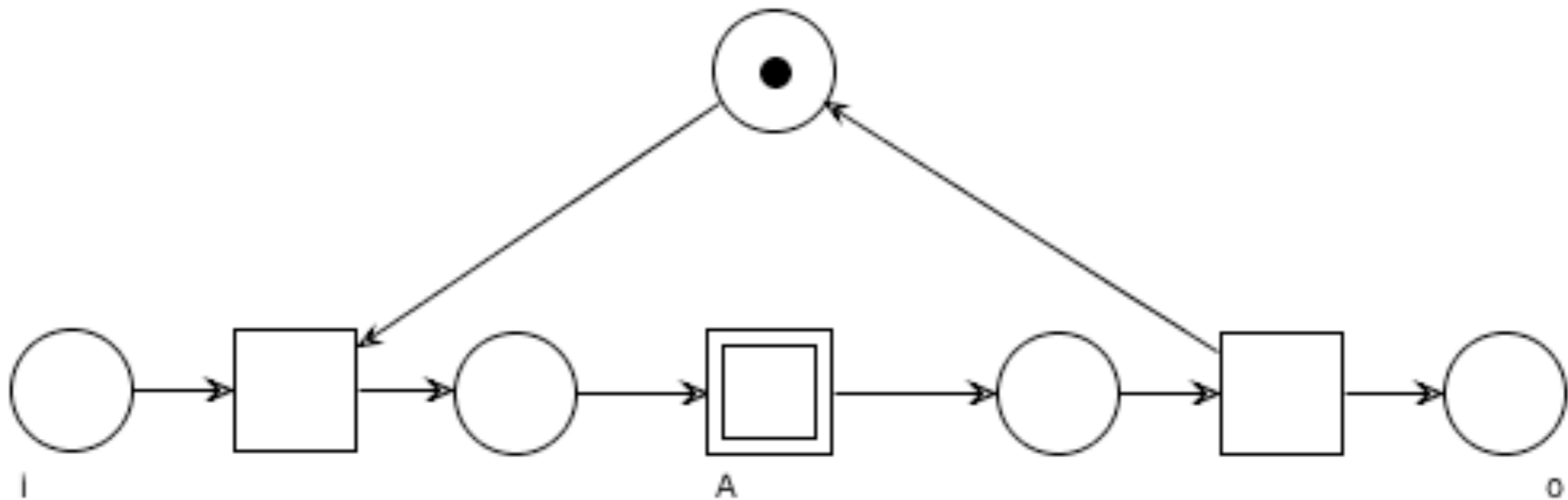
# Zero-or-more iteration (simplified version)

Decorated version for business process stakeholders



# One serve per time

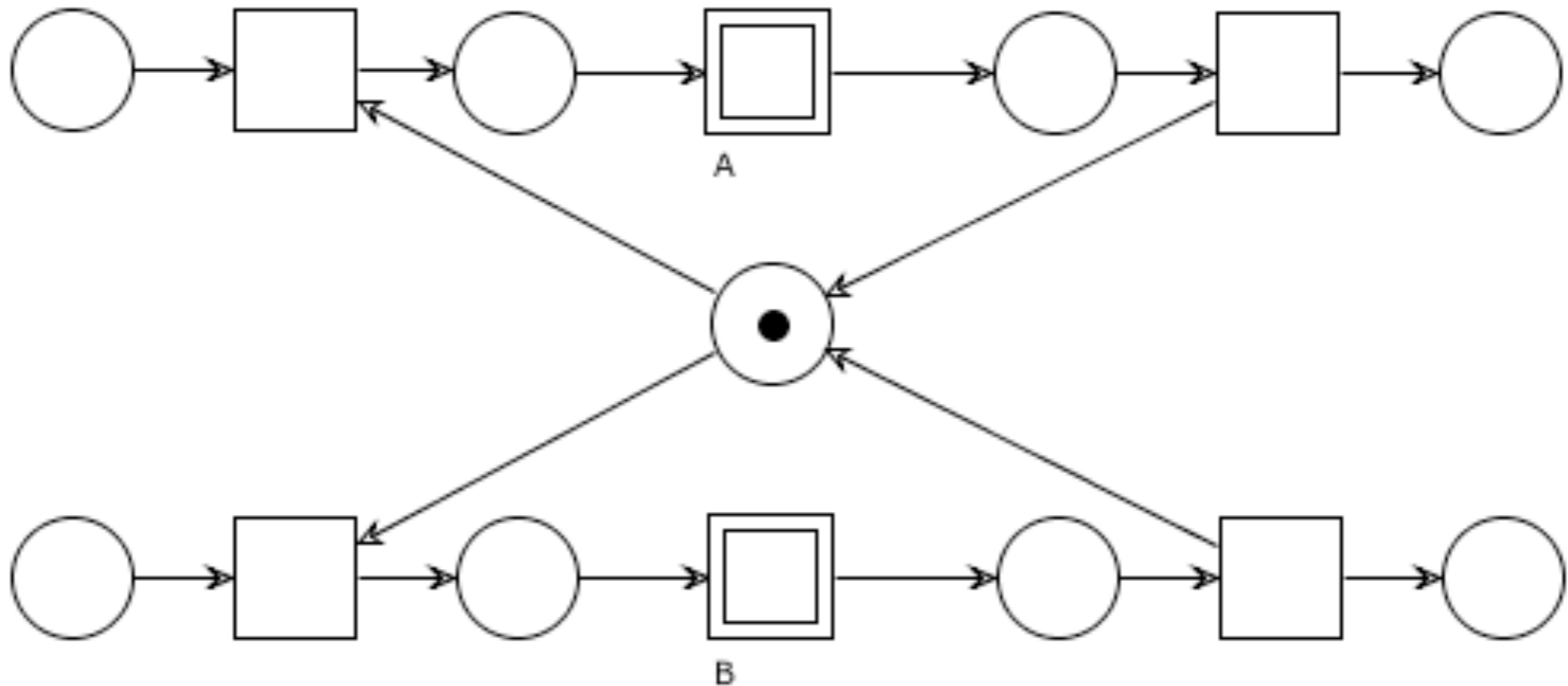
Multiple activations are handled one by one





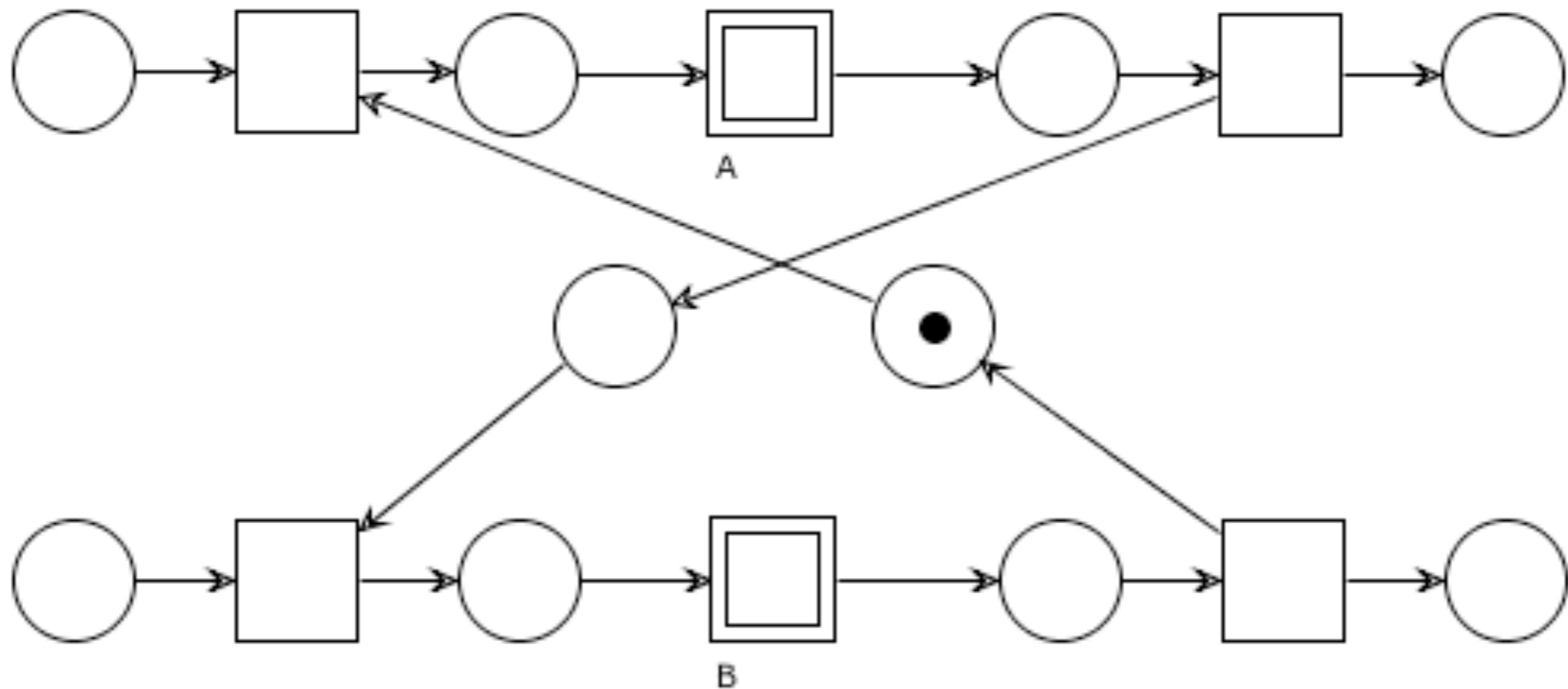
# Mutual exclusion

A and B cannot execute concurrently



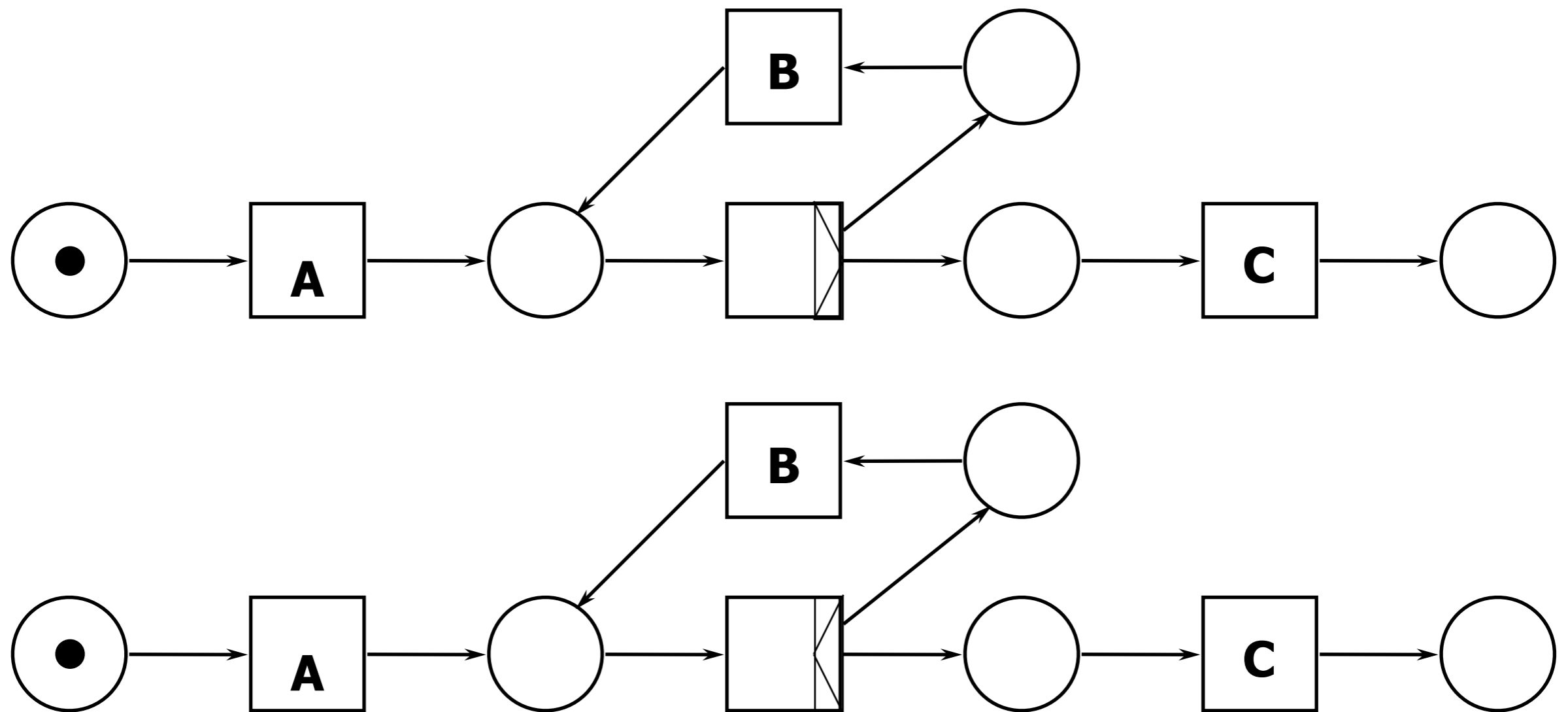
# Alternation

A and B execute one time each (A first)



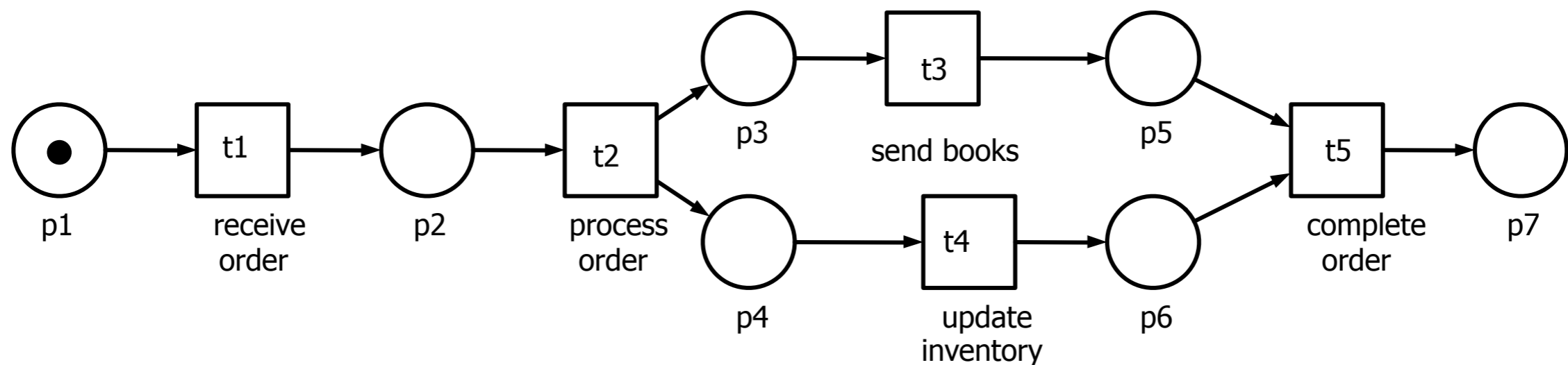
# Question time

What's the difference (also in terms of firing sequences)?



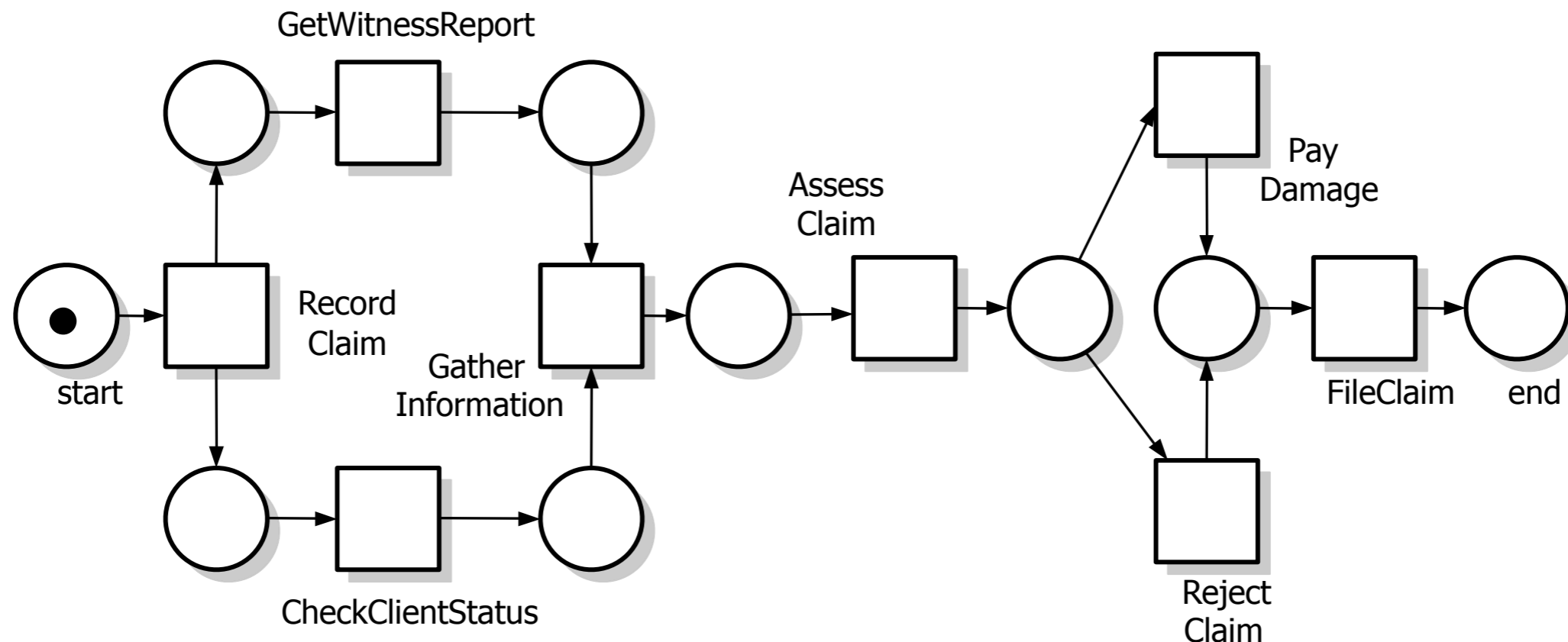
# Exercises

- Which "patterns" can be found in the workflow net below?
- "Sugarize" the net
- Draw the corresponding Reachability Graph
- What are the possible firing sequences?



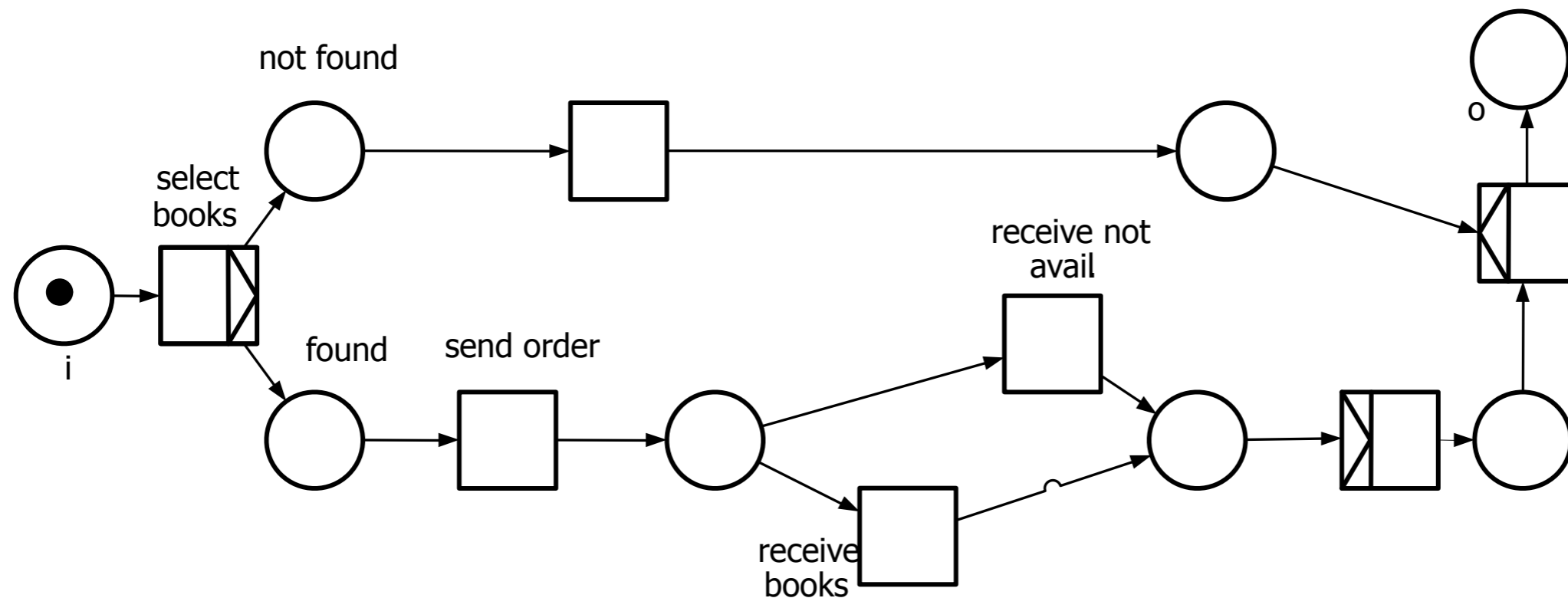
# Exercises

- Which "patterns" can be found in the workflow net below?
- "Sugarize" the net (where it makes sense)
- Name all places and draw the Reachability Graph



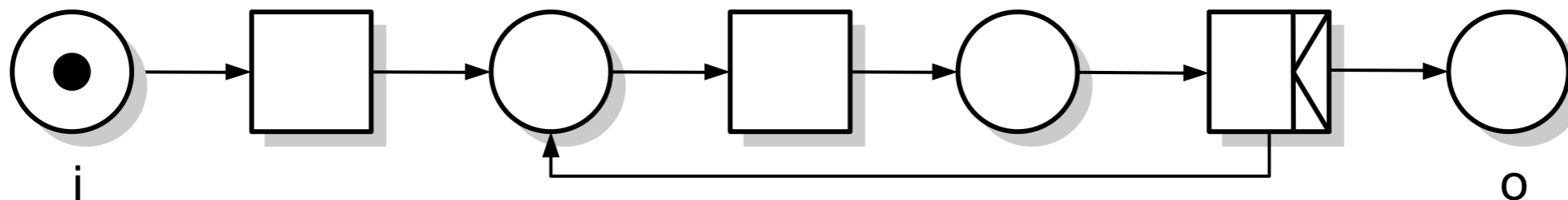
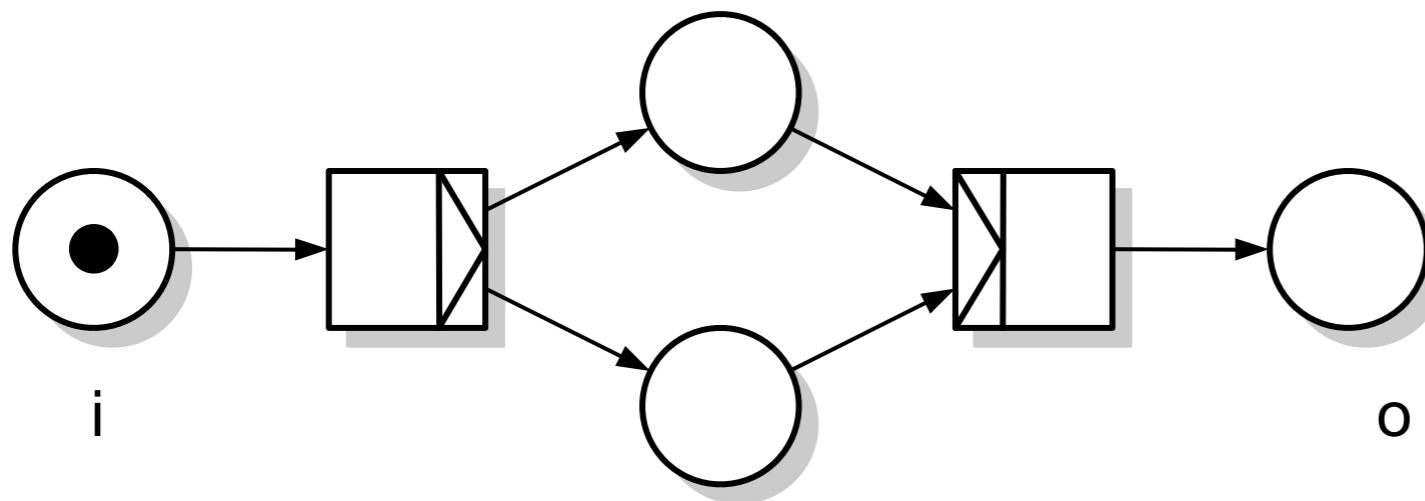
# Exercises

- "Desugarize" the workflow net below, then name all places and all transitions
- Draw the corresponding Reachability Graph
- What are the possible firing sequences?



# Exercises

- "Desugarize" the workflow nets below, then name all items
- Draw the corresponding Reachability Graphs
- What are their possible firing sequences?



# Triggers

Execution constraints can depend on the environment in which processes are enacted.

In the contexts of workflow nets, transitions can be annotated with the information on who (or what) is responsible for the "firing" of that task.

All transitions that are not annotated can fire automatically

Such annotations are called **triggers**



# Triggers

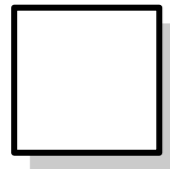
Triggers can be:

a human interaction

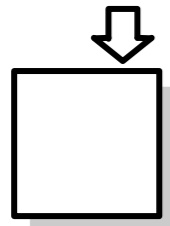
the receipt of a message

the expiration of a time-out

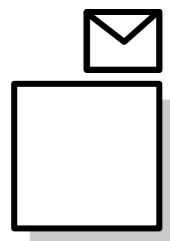
# Symbols for triggers



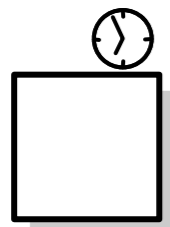
Automatic Trigger: Task enacted automatically



User Trigger: A human user takes initiative and starts activity

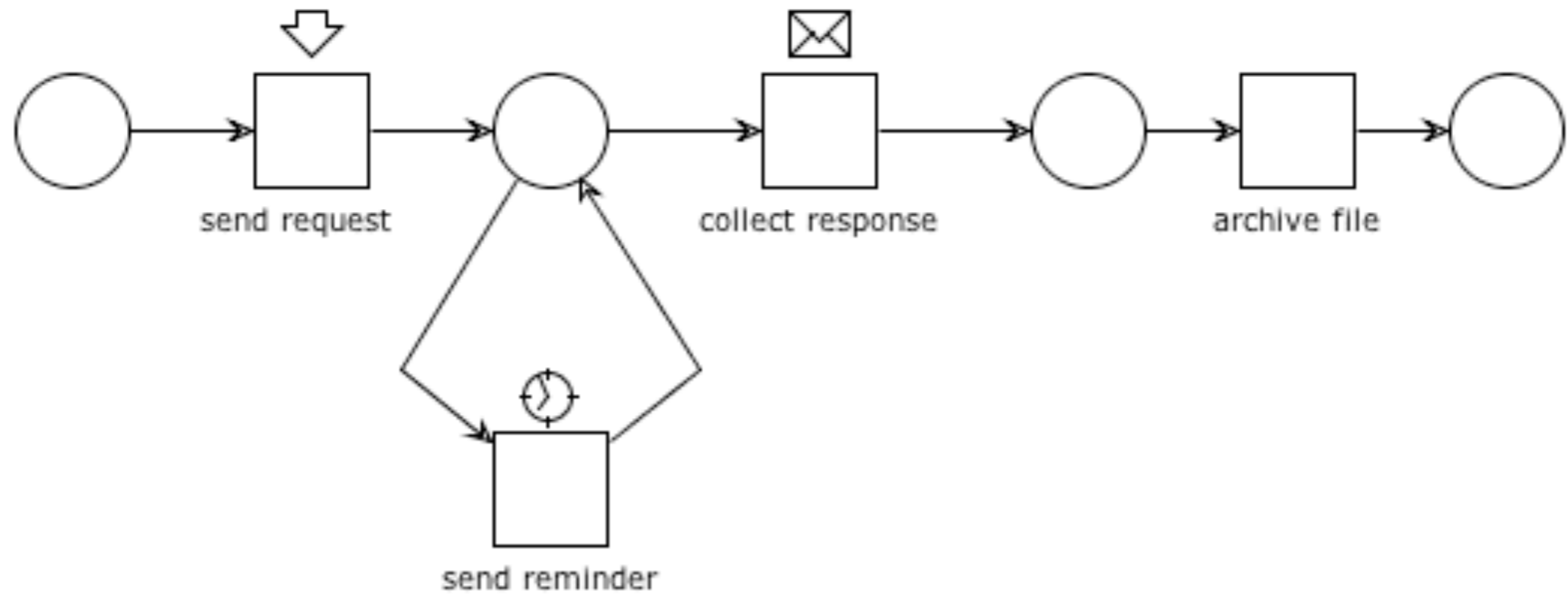


External Trigger: External event required to start activity

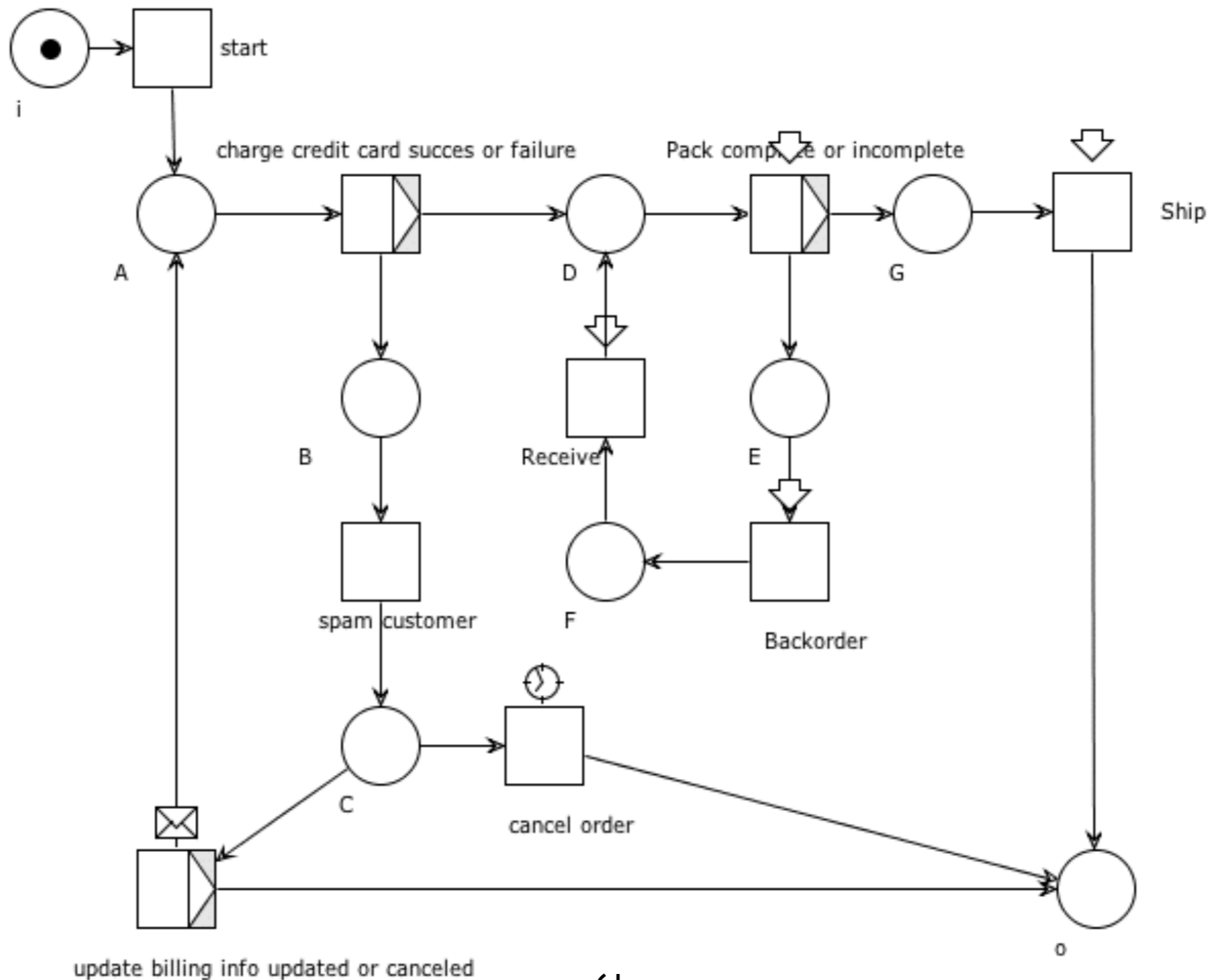


Time Trigger: Activity started when timer elapses

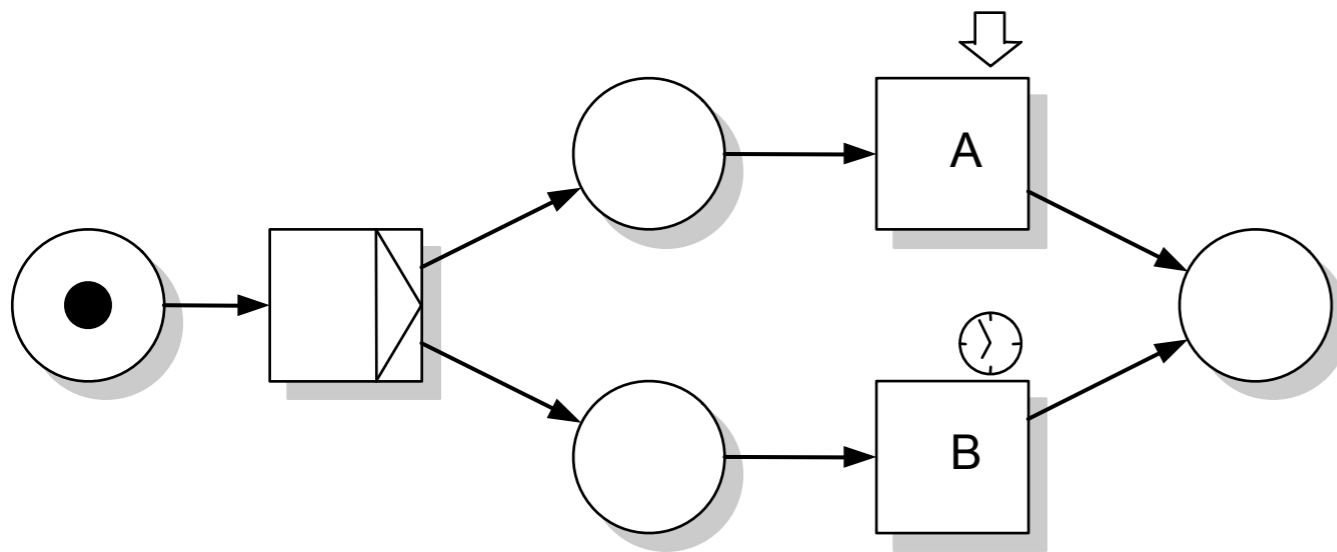
# Triggers: example



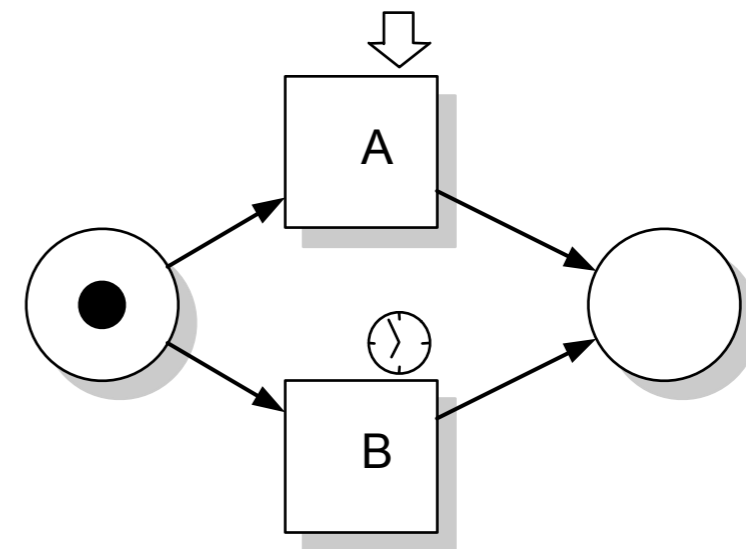
# Triggers: example



# Explicit vs Implicit XOR-split



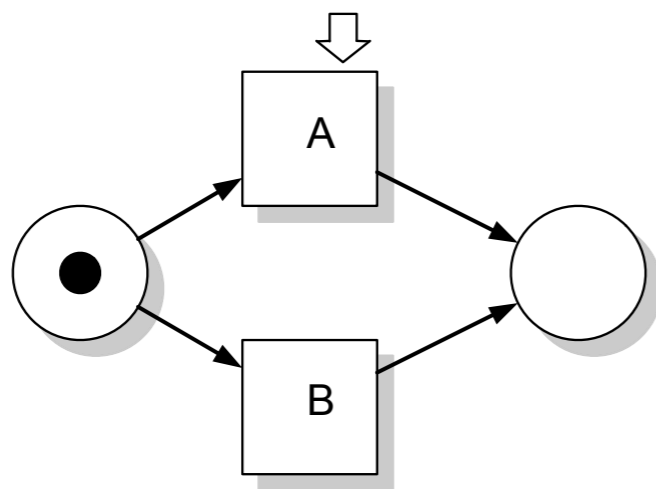
(a) *Explicit xor split* does not enable A and B concurrently



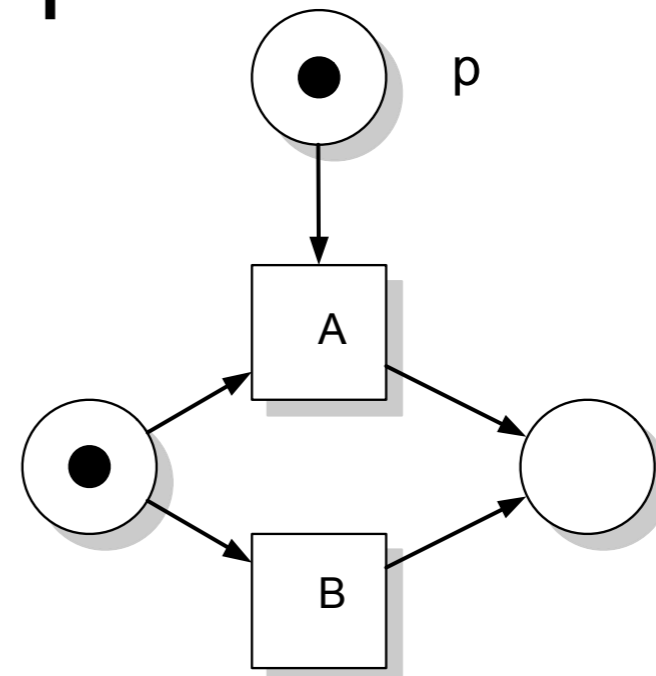
(b) *Implicit xor split* enables A and B concurrently

# Encoding triggers

Trigger activities can formally be represented by places with an arc to the respective transition...



(a) Transition A started by user trigger



(b) Representation of user trigger by additional place and additional arc

but such nets would not be workflow nets!  
(unless the resource is allocated at the beginning and deallocated at the end)

# Terminology: revisited

**task:** A logical step which may be executed for many cases

**work item** = task + case

A logical step which may be executed for a specific case

**activity** = task + case + (trigger) + (resource)

The actual execution of a task for a specific case

(work items and activities are task instances)

# Motivation for the analysis

Old BPs generally had simple structures and a physical document linked to each case (a sort of token that serializes tasks)

ICT developments (databases and networks) allowed terrific enhancements... and dangers

information is shared

parallelization is possible

completion times can be shortened

BPs are larger, with increasing complexity

flawed situations are more frequent



# Is this WF net ok?

