

Web Mining ed Analisi delle Reti Sociali

Mining on Complex (Social) Network


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Social Network Analysis

- Social Network Introduction
- Statistics and Probability Theory
- Models of Social Network Generation
- Mining on Social Network 
- Summary

Information on the Social Network

- Heterogeneous, multi-relational data represented as a graph or network
 - Nodes are objects
 - May have different kinds of objects
 - Objects have attributes
 - Objects may have labels or classes
 - Edges are links
 - May have different kinds of links
 - Links may have attributes
 - Links may be directed, are not required to be binary
- Links represent relationships and interactions between objects - rich content for mining

What is New for Link Mining Here

- Traditional machine learning and data mining approaches assume:
 - A random sample of homogeneous objects from single relation
- Real world data sets:
 - Multi-relational, heterogeneous and semi-structured
- Link Mining
 - Newly emerging research area at the intersection of research in social network and link analysis, hypertext and web mining, graph mining, relational learning and inductive logic programming

A Taxonomy of Common Link Mining Tasks



- Object-Related Tasks
 - Link-based object ranking
 - Link-based object classification
 - Object clustering (group detection)
 - Object identification (entity resolution)
- Link-Related Tasks
 - Link prediction
- Graph-Related Tasks
 - Subgraph discovery
 - Graph classification
 - Generative model for graphs

What Is a Link in Link Mining?

- Link: relationship among data
- Two kinds of linked networks
 - homogeneous vs. heterogeneous
- Homogeneous networks
 - Single object type and single link type
 - Single model social networks (e.g., friends)
 - WWW: a collection of linked Web pages
- Heterogeneous networks
 - Multiple object and link types
 - Medical network: patients, doctors, disease, contacts, treatments
 - Bibliographic network: publications, authors, venues

Link-Based Object Ranking (LBR)

- LBR: Exploit the link structure of a graph to order or prioritize the set of objects within the graph
 - Focused on graphs with single object type and single link type
- This is a primary focus of link analysis community
- Web information analysis
 - PageRank and Hits are typical LBR approaches
- In social network analysis (SNA), LBR is a core analysis task
 - Objective: rank individuals in terms of “centrality”
 - Degree centrality vs. eigen vector/power centrality
 - Rank objects relative to one or more relevant objects in the graph vs. ranks object over time in dynamic graphs

PageRank: Capturing Page Popularity (Brin & Page'98)



- Intuitions
 - Links are like citations in literature
 - A page that is cited often can be expected to be more useful in general
- PageRank is essentially “citation counting”, but improves over simple counting
 - Consider “indirect citations” (being cited by a highly cited paper counts a lot...)
 - Smoothing of citations (every page is assumed to have a non-zero citation count)
- PageRank can also be interpreted as random surfing (thus capturing popularity)

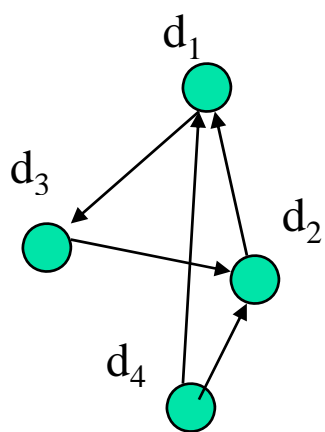
The PageRank Algorithm (Brin & Page'98)

Random surfing model:

At any page,

With prob. α , randomly jumping to a page

With prob. $(1 - \alpha)$, randomly picking a link to follow



$$M = \begin{bmatrix} 0 & 0 & 1/2 & 1/2 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 1/2 & 1/2 & 0 & 0 \end{bmatrix}$$

“Transition matrix”

Same as α/N (why?)

$$p_{t+1}(d_i) = (1 - \alpha) \sum_{d_j \in IN(d_i)} m_{ji} p_t(d_j) + \alpha \sum_k \frac{1}{N} p_t(d_k)$$

$$p(d_i) = \sum_k \left[\frac{1}{N} \alpha + (1 - \alpha) m_{ki} \right] p(d_k)$$

Stationary (“stable”) distribution, so we ignore time

$$\bar{p} = (\alpha I + (1 - \alpha) M)^T \bar{p} \quad \mathbf{I}_{ij} = 1/N$$

Initial value $p(d)=1/N$

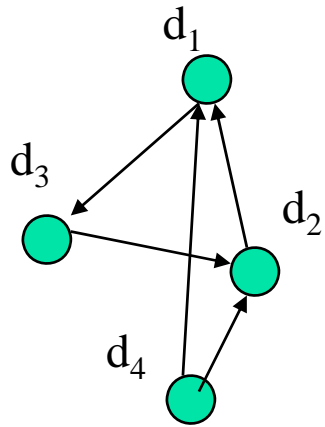
Iterate until converge

Essentially an eigenvector problem....

HITS: Capturing Authorities & Hubs (Kleinberg'98)

- Intuitions
 - Pages that are widely cited are good authorities
 - Pages that cite many other pages are good hubs
- The key idea of HITS
 - Good authorities are cited by good hubs
 - Good hubs point to good authorities
 - Iterative reinforcement ...

The HITS Algorithm (Kleinberg 98)



$$A = \begin{bmatrix} 0 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 \end{bmatrix}$$

“Adjacency matrix”

Initial values: $a=h=1$

$$h(d_i) = \sum_{d_j \in OUT(d_i)} a(d_j)$$

$$a(d_i) = \sum_{d_j \in IN(d_i)} h(d_j)$$

Iterate

Normalize:

$$\bar{h} = A\bar{a}; \quad \bar{a} = A^T\bar{h}$$

$$\bar{h} = AA^T\bar{h}; \quad \bar{a} = A^T A\bar{a}$$

$$\sum_i a(d_i)^2 = \sum_i h(d_i)^2 = 1$$

Again eigenvector problems...

Block-level Link Analysis (Cai et al. 04)

- Most of the existing link analysis algorithms, e.g. PageRank and HITS, treat a web page as a single node in the web graph
- However, in most cases, a web page contains multiple semantics and hence it might not be considered as an atomic and homogeneous node
- Web page is partitioned into blocks using the vision-based page segmentation algorithm
- extract page-to-block, block-to-page relationships
- Block-level PageRank and Block-level HITS

Link-Based Object Classification (LBC)

- Predicting the category of an object based on its attributes, its links and the attributes of linked objects
- **Web**: Predict the category of a web page, based on words that occur on the page, links between pages, anchor text, html tags, etc.
- **Citation**: Predict the topic of a paper, based on word occurrence, citations, co-citations
- **Epidemics**: Predict disease type based on characteristics of the patients infected by the disease
- **Communication**: Predict whether a communication contact is by email, phone call or mail

Challenges in Link-Based Classification

- Labels of related objects tend to be correlated
- Collective classification: Explore such correlations and jointly infer the categorical values associated with the objects in the graph
- Ex: Classify related news items in Reuter data sets (Chak'98)
 - Simply incorp. words from neighboring documents: not helpful
- Multi-relational classification is another solution for link-based classification

Group Detection

- Cluster the nodes in the graph into groups that share common characteristics
 - **Web:** identifying communities
 - **Citation:** identifying research communities
- Methods
 - Hierarchical clustering
 - Blockmodeling of SNA
 - Spectral graph partitioning
 - Stochastic blockmodeling
 - Multi-relational clustering

Entity Resolution

- Predicting when two objects are the same, based on their attributes and their links
- Also known as: deduplication, reference reconciliation, co-reference resolution, object consolidation
- Applications
 - **Web**: predict when two sites are mirrors of each other
 - **Citation**: predicting when two citations are referring to the same paper
 - **Epidemics**: predicting when two disease strains are the same
 - **Biology**: learning when two names refer to the same protein

Entity Resolution Methods

- Earlier viewed as pair-wise resolution problem: resolved based on the similarity of their attributes
- Importance at considering links
 - Coauthor links in bib data, hierarchical links between spatial references, co-occurrence links between name references in documents
- Use of links in resolution
 - Collective entity resolution: one resolution decision affects another if they are linked
 - Propagating evidence over links in a depen. graph
 - Probabilistic models interact with different entity recognition decisions

Link Prediction



- Predict whether a link exists between two entities, based on attributes and other observed links
- Applications
 - **Web**: predict if there will be a link between two pages
 - **Citation**: predicting if a paper will cite another paper
 - **Epidemics**: predicting who a patient's contacts are
- Methods
 - Often viewed as a binary classification problem
 - Local conditional probability model, based on structural and attribute features
 - Difficulty: sparseness of existing links
 - Collective prediction, e.g., Markov random field model

Link Cardinality Estimation

- Predicting the number of links to an object
 - **Web**: predict the authority of a page based on the number of in-links; identifying hubs based on the number of out-links
 - **Citation**: predicting the impact of a paper based on the number of citations
 - **Epidemics**: predicting the number of people that will be infected based on the infectiousness of a disease
- Predicting the number of objects reached along a path from an object
 - **Web**: predicting number of pages retrieved by crawling a site
 - **Citation**: predicting the number of citations of a particular author in a specific journal

Subgraph Discovery

- Find characteristic subgraphs
 - Focus of graph-based data mining
- Applications
 - **Biology:** protein structure discovery
 - **Communications:** legitimate vs. illegitimate groups
 - **Chemistry:** chemical substructure discovery
- Methods
 - Subgraph pattern mining
- Graph classification
 - Classification based on subgraph pattern analysis

Metadata Mining



- Schema mapping, schema discovery, schema reformulation
- **cite** - matching between two bibliographic sources
- **web** - discovering schema from unstructured or semi-structured data
- **bio** - mapping between two medical ontologies

Link Mining Challenges

- Logical vs. statistical dependencies
- Feature construction
- Instances vs. classes
- Collective classification
- Collective consolidation
- Effective use of labeled & unlabeled data
- Link prediction
- Closed vs. open world

Challenges common to any link-based statistical model (Bayesian Logic Programs, Conditional Random Fields, Probabilistic Relational Models, Relational Markov Networks, Relational Probability Trees, Stochastic Logic Programming to name a few)

Logical vs. Statistical Dependence

- Coherently handling two types of dependence structures:
 - Link structure - the logical relationships between objects
 - Probabilistic dependence - statistical relationships between attributes
- Challenge: statistical models that support rich logical relationships
- Model search complicated by the fact that attributes can depend on arbitrarily linked attributes -- issue: how to search this huge space

Feature Construction



- In many cases, objects are linked to a **set** of objects. To construct a single feature from this set of objects, we may either use:
 - Aggregation
 - Selection

Individuals vs. Classes

- Does model refer
 - explicitly to individuals
 - classes or generic categories of individuals
- On one hand, we'd like to be able to model that a connection to a particular individual may be highly predictive
- On the other hand, we'd like our models to generalize to new situations, with different individuals

Collective Classification



- Using a link-based statistical model for classification
- Inference using learned model is complicated by the fact that there is correlation between the object labels

Collective Consolidation



- Using a link-based statistical model for object consolidation
- Consolidation decisions should not be made independently

Labeled & Unlabeled Data

- In link-based domains, unlabeled data provide three sources of information:
 - Helps us infer object attribute distribution
 - Links between unlabeled data allow us to make use of attributes of linked objects
 - Links between labeled data and unlabeled data (training data and test data) help us make more accurate inferences


Link Prior Probability

- The prior probability of any particular link is typically extraordinarily low
- For medium-sized data sets, we have had success with building explicit models of link existence
- It may be more effective to model links at higher level--required for large data sets

Closed World vs. Open World

- The majority of SRL approaches make a closed world assumption, which assumes that we know all the potential entities in the domain
- In many cases, this is unrealistic
- Work by Milch, Marti, Russell on BLOG

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